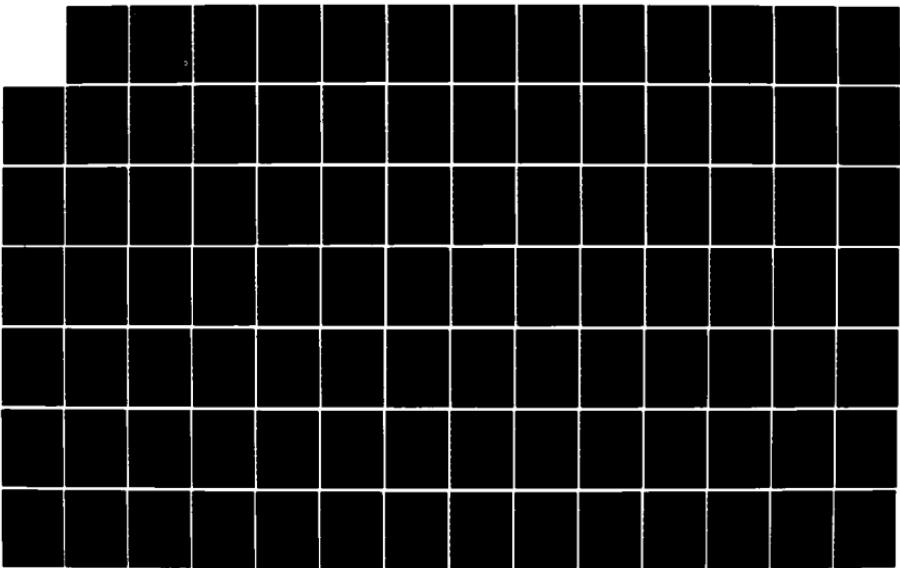
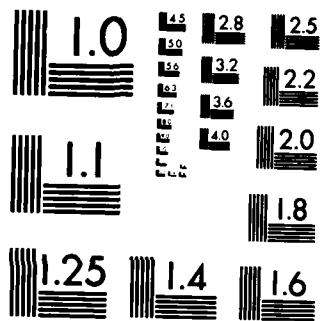


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ANALYSIS OF SPACE DIVERSITY TECHNIQUES
FOR EHF SATELLITE DOWNLINKS

THESIS

Steven L. Skipper
Captain, USAF

AFIT/GE/ENG/84D-61

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ANALYSIS OF SPACE DIVERSITY TECHNIQUES
FOR EHF SATELLITE DOWNLINKS

THESIS

Presented to the Faculty of the School of Engineering
of the Air Force Institute of Technology
Air University
In Partial Fulfillment of the
Requirements for the Degree of
Master of Science in Electrical Engineering

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Steven L. Skipper, B.S.

Captain, USAF

December 1984

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Preface

The purpose of this study was to investigate different techniques for selecting the optimum downlink signal received by spatially diverse earth stations operating in the extremely high frequency (EHF) band. Space diversity configurations can be used to overcome the attenuation effects of rainfall, which can be very severe for frequencies above 10 GHz. Thus, special consideration must be given to the parameters and methods used to determine the optimum received signal when employing a space diversity reception system. This report is limited in scope to the development of three linear diversity combining techniques. The theoretical analysis and development of each of these techniques can be fully understood by the reader with a background in probability theory and digital signaling techniques.

I would like to thank Mr. Richard A. Williams of the Defense Communications Engineering Center (DCEC) for proposing this project. Gratitude is also due to Captain Jim Frazier, also from DCEC, for his assistance in arranging our visits to DCEC. Special thanks to my faculty advisor, Major Kenneth G. Castor of the Air Force Institute of Technology, for his guidance and understanding that greatly aided me in the completion of this study.

Steven L. Skipper

Table of Contents

	Page
Preface	ii
List of Figures	v
List of Tables	vi
Abstract	vii
I. Introduction	1
Background	1
Problem	5
Scope	5
Assumptions	5
Summary of Current Knowledge	6
Standards	6
Approach	7
II. Satellite Background Information	8
Antenna Gain	8
EIRP	10
External Noise	12
Atmospheric Losses	12
Water Vapor and Molecular Oxygen	12
Attenuation	13
Rainfall Attenuation Effects	13
Types of Rain	14
Receiver Noise	16
Noise Temperature	16
Noise Figure	17
Carrier-To-Noise Ratios (CNR)	18
Power Link Equations	19
Digital Signaling Methods for Satellite Communications Systems	21
Multiphase Signaling Waveforms	23
Performance of M-ary PSK	25
Differentially Encoded PSK (DPSK)	26
Performance of DPSK	26
III. Rainfall Characteristics	28
Rainfall Physical Structure Characteristics	28
Rain Rates	29
Rain Scattering	33

	Page
Rain Attenuation Models	33
Statistical Behavior of Rain	35
IV. Diversity Techniques For Satellite Communications	42
Description of Basic Diversity System	42
Bit Stream Synchronization	46
Linear Diversity Combining Techniques	47
Space Diversity Measurements	48
Diversity Performance Assessment Techniques	50
V. Analysis of Selected Linear Diversity Combining Techniques	57
Considerations for Bit Error Analysis	57
Assumptions for Diversity Analysis	61
Probability of Error in Rayleigh Channel with No Diversity	63
Selection Diversity	64
Analysis of Selection Diversity	64
Equal Gain Diversity	68
Analysis of Equal Gain Diversity	68
Maximal Ratio	70
Analysis of Maximal Diversity	72
VI. Computer Program Development	76
Choice of Range of Variables	76
Equations Used to Calculate Probability of Bit Error	77
Solving the Indefinite Integral	78
Validation of Computer Results	79
Computer Program for Calculation of Rain Attenuation	80
VII. Results	81
Analysis of Diversity Benefits	81
Analysis of Rain Attenuation for Downlink	83
VIII. Conclusions and Recommendations	99
Conclusions	99
Recommendations	100
Bibliography	101
Vita	103

List of Figures

Figure	Page
1.1 Types of Satellite Systems	2
1.2 Using Space Diversity in a Satellite System . . .	4
2.1 Digital Communications Block Diagram	22
3.1 Cumulative Distribution Function (C.D.F.) of Rain Rates for 20 U.S. Locations During the Period 1966 to 1970; Based on One-Minute Intervals	30
4.1 Angle Diversity	44
4.2 Block Diagram--Downlink Space Diversity	45
4.3 Technique for Calculating Diversity Improvement and Diversity Gain for Single-Site and Space Diversity Cumulative Fading Statistics	51
5.1 Gray Code for 8-ary PSK.	60
5.2 Selection Diversity	65
5.3 Equal Gain Diversity	68
5.4 Maximal Ratio Diversity	71
5.5 4-ary Gray Code.	74
7.1 DQPSK and 8-ary PSK w/No Diversity	86
7.2 Selection Diversity w/DQPSK	87
7.3 Selection Diversity w/8-ary PSK	88
7.4 Equal Gain Diversity w/DQPSK	89
7.5 Equal Gain Diversity w/8-ary PSK	90
7.6 Maximal Ratio Diversity w/DQPSK	91
7.7 Maximal Ratio Diversity w/8-ary PSK	92
7.8 Rain Attenuation Using $A = aR^b$ Relationship. . .	97
7.9 Effective Path Length for Rain Rates	98

List of Tables

Table	Page
3.1 Measured Raindrop Terminal Velocities and Dropsize Distributions at Ground Level	32
3.2 Regression Calculations For a and b in $A = aR^b$ (dB/km) as Functions of Frequency and Dropsize Distribution with Rain Temperature = 20°C	36
3.3 Regression Calculations For a and b in $A = aR^b$ (dB/km) as Functions of Frequency and Dropsize Distribution with Rain Temperature = 0°C	37
3.4 Regression Calculations for a and b in $A = aR^b$ (dB/km) as Functions of Frequency and Dropsize Distribution with Rain Temperature = -10°C.	38
4.1 Measurement Techniques for Obtaining Slant Path Attenuation	49
7.1 Comparison of Selected Diversity Techniques w/DQPSK to DQPSK w/No Diversity	93
7.2 Comparison of Selected Diversity Techniques w/8-ary PSK to 8-ary PSK w/No Diversity	94
7.3 Comparison of Selected Diversity Techniques w/DQPSK with Respect to Probability of Bit Error	95
7.4 Comparison of Selected Diversity Techniques w/8-ary PSK with Respect to Probability of Bit Error	96

Abstract

This study investigated some of the diversity combining techniques that can be used with a space diversity downlink reception configuration to overcome the attenuation effects of rainfall. The diversity combining techniques selected for development and analysis were selection, equal gain, and maximal ratio combining. Each of these techniques were considered with two different digital signaling schemes, 8-ary phase-shift keying (PSK) and differentially encoded quadrature PSK (DQPSK), to form six distinct diversity technique/signaling scheme combinations.

The analysis was accomplished by deriving the probability of bit error functions for 8-ary PSK and DQPSK and by developing the probability of density functions for each diversity technique under the assumption of a slowly fading Rayleigh channel. By taking the integral from zero to infinity of the product of the two functions for each diversity technique/signaling scheme combination, the probability of bit error was calculated for each specified combination. The number of channels in the diversity system was varied to illustrate the trade-off between the improvement of bit error performance and cost. The results show the theoretical benefits attributed to the diversity combining techniques that can be employed in satellite communications systems. Additionally, information is provided to estimate the rain attenuation

given the rain rate so that its effects on bit error performance can be obtained and compared to the case of no rain attenuation.

ANALYSIS OF SPACE DIVERSITY TECHNIQUES
FOR EHF SATELLITE DOWNLINKS

I. Introduction

Background

The use of orbiting satellites has become an integral part of our world-wide communications and military command, control, and communications systems. A satellite communications system can be categorized as one of three basic types shown in Figure 1.1. System I shows an uplink from a ground-based earth station to the satellite, and a downlink from the satellite back to the destination earth station. The function of the satellite is to collect the electromagnetic fields from the signal transmitted by the sending earth station and retransmit the received signal to the other earth station.

System II shows a satellite crosslink between two satellites prior to the downlink transmission. System III shows a satellite relay system involving an earth station, a near-earth user (aircraft, ship, etc.) and a satellite. The system III configuration is of particular importance since it has many military applications. Regardless of which system configuration is employed, there are several atmospheric effects that can degrade the transmitted signal strength and reduce the capability of transmitting information via satellite.

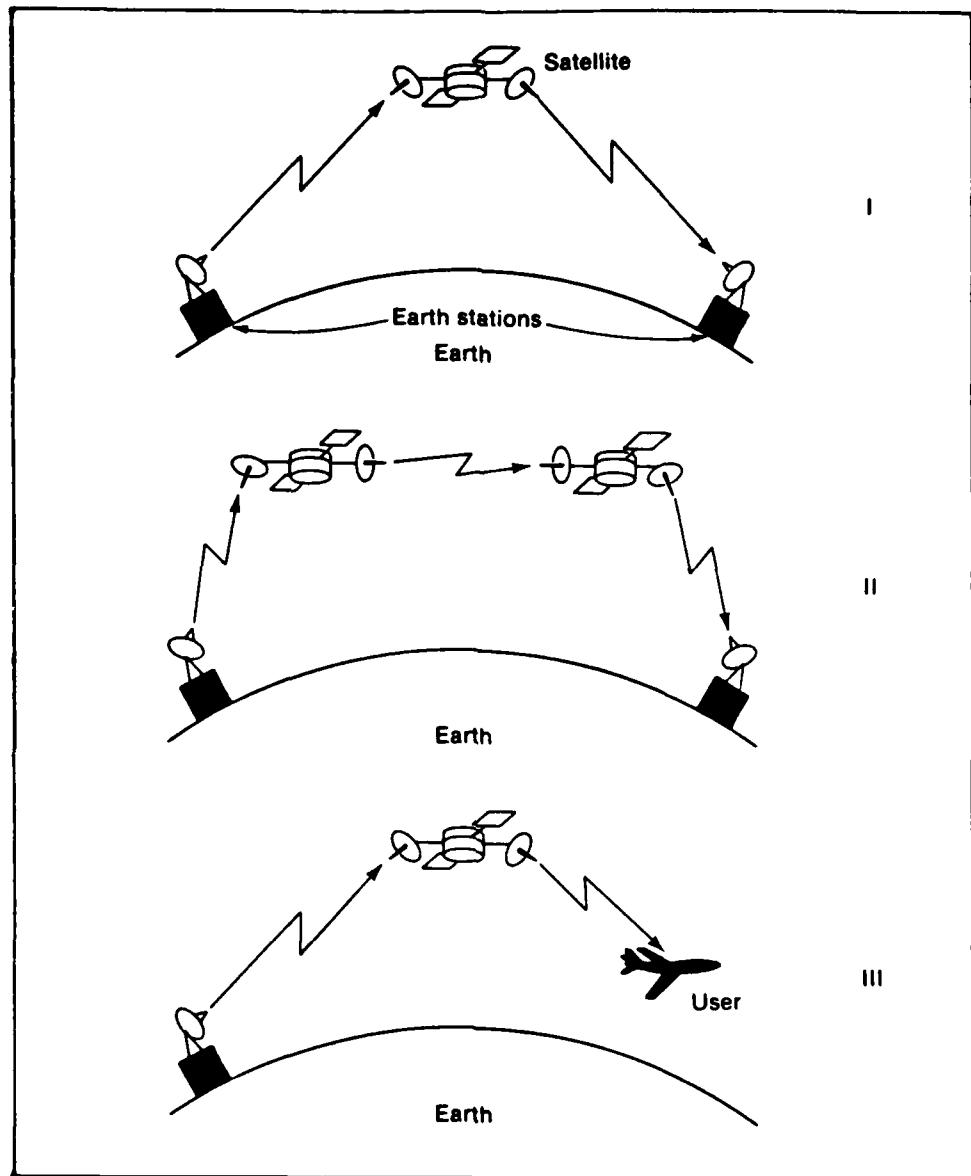


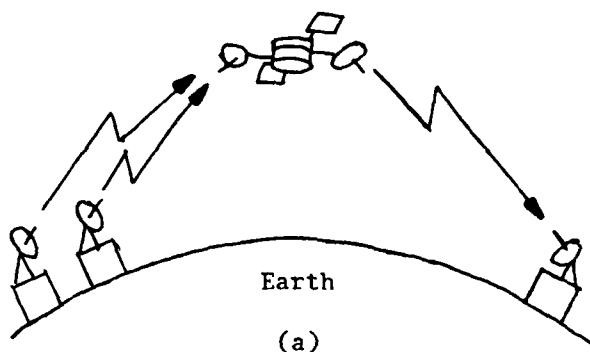
Figure 1.1 Types of Satellite Systems

- I Ground-ground
- II Ground-crosslink-ground
- III Ground-user relay

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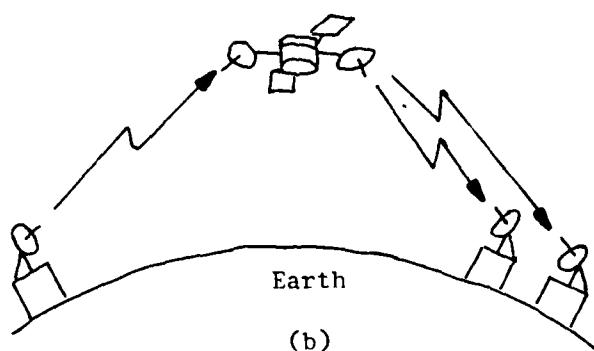
The most serious of these atmospheric effects to a satellite communications link is rainfall, which affects both uplink and downlink transmissions (11:96). Rain effects become more severe at wavelengths that approach the water drop size, which is dependent on the type of rainfall. In heavy rains as raindrop size increases, severe absorption occurs in the extremely high frequency (EHF) band, the range where many existing satellites operate. Therefore, in the EHF band, there is a potential for significantly more signal attenuation during rain as compared to the attenuation caused during clear weather conditions.

Generally, the solution to maintaining the satellite communications link is to add enough extra power (power margin) to transmit the signal over the maximum additional attenuation caused by rain. However, to maintain a highly reliable link in the EHF band, the cost of providing sufficient power margin with current technology becomes prohibitive and may not be technically feasible. One alternative for improving reliability is to spatially separate two or more earth stations since they are not likely to experience simultaneous fading from the same rainstorm (See Figure 1.2). For the uplink transmission, all earth station transmit the same signal and the optimum received signal (i.e., the signal with the least amount of attenuation) is chosen at the satellite and retransmitted. For the downlink reception, earth stations receive the transmitted signal from the satellite



(a)

Space Diversity in Uplink



(b)

Space Diversity in Downlink

Figure 1.2 Using Space Diversity in a Satellite System

simultaneously and the optimum signal is selected and then retransmitted to terrestrial destinations.

Problem

When using a space diversity configuration to overcome the attenuation effects of rainfall, some consideration must be given to the parameters and the methods used to determine the optimum received signal. The purpose of this research is to investigate techniques for selecting the optimum signal from signals received by spatially diverse earth stations operating in the EHF band (i.e., the case of Figure 1.2b).

Scope

The scope of this research will be limited to an investigation of methods to determine the optimum signal received by two or more spatially diverse earth stations from the satellite downlink transmissions. Different methods of selecting the optimum signal will be investigated and developed. After a theoretical analysis of each selection method, a computer program will be developed to simulate the operational environment and verify the best method for choosing the optimum received downlink signal in a space diversity configuration system. Costs associated with the development of the proposed methods for signal selection will not be examined.

Assumptions

The following assumptions are made throughout this research project:

1. A satellite beacon is available.
2. All uplink transmissions are at 30 GHz and the down-link transmissions are at 20 GHz.
3. The focus of this report will be on satellite systems using diversity techniques to improve downlink reception performance as depicted in Figure 1.2b.
4. Digital signaling schemes used will be 8-ary Phase-Shift Keying (PSK) and Differentially encoded Quadrature PSK (DQPSK).

These assumptions are established to model a generic satellite system for military applications that could easily be developed and deployed using current satellite system technology and practices.

Summary of Current Knowledge

The use of space diversity to combat atmospheric attenuation in satellite communications links is a well known concept that has been thoroughly researched and documented during the past 10-12 years (1,9). This research project will attempt to establish a model for space diversity gain by using well known linear diversity combining techniques and giving consideration to the spatial separation of the earth stations.

Standards

The criterion used to measure the performance of each signal selection scheme will be the probability of bit error (P_e) versus the average signal-to-noise ratio (SNR) per bit, γ_b , of the received downlink signal. This measurement is

the standard criterion for comparing the performances of digital communications systems. These values, (P_e vs. γ_b), will be calculated and plotted for each selection scheme during the computer simulation. These results will allow for a direct comparison of all of the developed signal selection schemes and a measurement of the benefits derived from using space diversity transmission schemes as compared to the result from the use of a standard satellite system without space diversity.

Approach

A detailed investigation of possible linear diversity combining techniques for optimum signal selection will be conducted to determine which methods are best suited for this satellite communications application. For each diversity technique, the criteria for determining the optimum received signal will be fully developed. After a complete development and analysis of each of the proposed diversity signal selection methods, a computer simulation will model the operational environment and provide a performance measurement for each diversity technique.

II. Satellite Background Information

The major elements in a satellite communications system include the satellite, a network of earth stations, and multiple-access communications equipment by which many earth stations can operate through a single satellite (22:131). A satellite communications link consists of a satellite orbiting in space and one or more earth stations. The performance of this communications link is greatly influenced by the earth-space propagation channel. One of the major differences between satellite links and terrestrial telecommunications is the distances that the carriers must be transmitted. Since the strength of the radiated signal diminishes with the square of the distance it travels, the satellite signals are relatively weak when received at the distant end. However, the amount of received carrier power determines the ability of the receiver to demodulate or decode the information (11:83). In satellite systems it is extremely important to know the key parameters that directly determine this received power so that these systems can be properly analyzed. Thus, an understanding of the basic power flow equations associated with satellite channels is necessary.

Antenna Gain

The antennas used in satellite links do not radiate equally in all directions but are designed to focus the radiation in a particular direction. The increase in power

achieved by focusing the antenna is referred to as the gain of the antenna. An isotropic antenna which radiates equally in all directions has an antenna gain = 1. The gain of the antenna, $G_t(\phi_z, \phi_\ell)$ is a function of the angular direction of the receiver, where (ϕ_z, ϕ_ℓ) refers to the azimuth and elevation angle, respectively, measured from a coordinate system centered at the transmitting antenna (11:83). Therefore, antennas can be characterized by their gain pattern $G_t(\phi_z, \phi_\ell)$ which indicates how the antenna gain is distributed spatially with respect to the antenna coordinate system.

The most important parameters of an antenna pattern are its gain (the maximum value of the gain pattern), its beamwidth (a measure of the angle in which most of the gain occurs), and its sidelobes (amount of gain in the off-axis direction) (11:87). For most satellite communications purposes, antenna patterns should be highly directional with most of the gain concentrated over a narrow beamwidth and a very small part of the radiated energy in the sidelobes. However, the gain and beamwidth is dependent on the type of antenna used.

The gain of a transmitting antenna is

$$G_t = \frac{\text{Power received from the antenna}}{\text{Power received if the radiation were isotropic}} \quad (2.1)$$

Although the antenna gain is dependent on the type of antenna used, a useful approximation for this gain is

$$G = \frac{24\pi A_t}{\lambda^2} \quad (2.2)$$

where

A_t = aperture cross-sectional area of transmitting antenna

Z = the efficiency of the antenna aperture

λ = wavelength of transmission

λ , the wavelength of the radiation, is inversely proportional to its frequency f :

$$\lambda = \frac{C}{f} \quad (2.3)$$

where C is the velocity of light. Thus, the antenna gain approximation can be written such that

$$G = \frac{Z4\pi f^2 A_t}{C^2} \quad (2.4)$$

where

$$C = 2.99 \times 10^8 \text{ meters/second}$$

It is obvious that the gain of the antenna is dependent on the frequency of transmission and the efficiency of the antenna aperture.

EIRP

The power of the transmitter is often referred to in a manner which takes the gain of the antenna into consideration. It is referred to as the effective isotropic radiated power (EIRP). EIRP is the power of a transmitter and isotropic antenna that would achieve the same result as the transmitter and antenna in question.

$$\text{EIRP} = P_t G_t (\phi_z, \phi_\lambda) \quad (2.5)$$

where

P_t = available antenna input carrier power from the transmitter power amplifier, including circuit coupling losses and antenna radiation losses

$G_t(\phi_z, \phi_\ell)$ = gain of transmitting antenna

Now we can define the received carrier power collected by the receive antenna that is normal to the transmitter as

$$P_r = \frac{(EIRP)L_a A_r}{4\pi Z^2} \quad (2.6)$$

where

L_a = atmospheric loss

A_r = the aperture of the receive antenna

$$= (\lambda^2/4\pi)G_r(\phi_z', \phi_\ell') \quad (2.7)$$

where

$G_r(\phi_z', \phi_\ell')$ = azimuth and elevation angles of the transmitter relative to the receiver coordinate system

λ = carrier wavelength

An equivalent expression for Eq (2.6) is

$$P_r = (EIRP)L_p L_a G_r(\phi_z', \phi_\ell') \quad (2.8)$$

where we define

$$L_p = (\lambda/4\pi D)^2 = (C/4\pi f D)^2$$

L_p is called the propagation or free space loss that is incurred by the communications link. It is dependent on the frequency, f , and the distance, D .

Eq (2.7) can also be restated in a more useful form where

$$(P_r)_{dB} = (EIRP)_{dB} + (L_p)_{dB} + (L_a)_{dB} + (G_r)_{dB} \quad (2.9)$$

External Noise

In addition to receiving the desired signal, the receiving antenna also gathers other forms of electromagnetic energy that may be present. These other radiations may be interference or noise that can distort the transmitted signal. The major external noises to a satellite communications link are:

1. Atmospheric Losses/Noise
2. Thermal Noise
3. Sky Noise
4. Galactic Noise
5. Cosmic Noise

The combination of all sources of interference form a total noise level for the receiving system of the satellite link (16:123).

Atmospheric Losses

There are many frequency dependent effects on the propagation channel, in addition to the free space loss, that increases the total transmission loss of the communications link (6:162). These propagation effects can be categorized as atmospheric losses. The primary causes of atmospheric losses for satellite communications links are:

1. uncondensed water vapor
2. molecular oxygen
3. rainfall

Water Vapor and Molecular Oxygen Attenuation. These two losses are relatively constant and easily calculated, although the attenuation levels vary within the carrier frequency. The main reason for the attenuation due to water vapor and molecular oxygen is that some of their associated atmospheric particles have molecular resonances in the microwave frequency band.

Below 10 GHz, atmospheric losses are minimal, (usually less than 2 dB); however, at higher frequencies, the attenuation begins to increase rapidly. The higher levels of attenuation occur at the frequencies having wavelengths corresponding to specific gas molecules in the atmosphere (11:94). Therefore, the attenuation caused by water vapor and oxygen varies greatly with the frequency. Severe attenuation due to water vapor molecules occurs at ~22 GHz while the severe attenuation due to oxygen molecules occurs at ~60 GH. Thus, the frequencies for the RF carrier for satellite links are chosen in the frequency range where these types of attenuation are minimized.

Rainfall Attenuation Effects. The effects of rainfall attenuation on satellite communications varies with frequency, however, it can have a severe effect on signal strength at frequencies above 10 GHz. Rainfall is the most serious atmospheric effect on a satellite link; therefore, special

consideration must be given to the effects of precipitation on the earth-space propagation path when designing a satellite communications system (8:2-1). At frequencies above 10 GHz, rain is known to cause significant attenuation, absorption, scattering, amplitude and phase scintillations, depolarization, and bandwidth decoherency. All of these phenomena combine to degrade the reliability of the satellite communications link. Its obvious impact on the satellite system is cost, since methods must be incorporated into the system to combat rainfall effects if uninterrupted service is desired (10:191).

Rainfall is a complicated subject primarily because of the complexity of the rainfall itself. Rainfall can assume many different forms depending on the geographical location, time of year, time of day, temperature, altitude, and other earth station site characteristics (8:2-1).

Types of Rain. As described in Ref 8, chapter 2, there are three basic types of rain: stratiform, convective, and cyclonic. In mid-latitude regions of the world, stratiform rain is a type of rain that primarily occurs in the spring and fall. It exhibits stratified horizontal extents of hundreds of kilometers (km), vertical heights of 4-6 km, with durations exceeding one hour and rain rates less than about 25 mm/hr (1 inch/hr). Stratiform rain has a rain rate and duration which often necessitates the use of link power margin to exceed the attenuation caused by a 25 mm/hr rain rate.

Convective rains are a result of vertical atmospheric motions producing vertical transport and mixing. The convective flow occurs in a cell whose horizontal extent is usually several kilometers. The cell usually extends to heights exceeding the freezing layer because of convective upwelling. The cell may be isolated or embedded in a thunder-storm associated with a weather front. Because of the motion of the front and the sliding motion of the cell along the front, the duration of high rain rate is usually only several minutes. This type of rain is the most common source of high rain rates in the U.S. and Canada.

Tropical cyclonic storms (hurricanes) occasionally pass along the U.S. eastern and southern coasts during August to October. These circular storms are typically 50-200 km in diameter, move at 10-20 km/hr, extend upward to 8 km, and have high rain rates that exceed 25 mm/hr.

Stratiform and cyclonic rainfall cover large geographic areas and the spatial distribution of total rainfall from such a storm is assumed to be uniform. Therefore, the rain rate averaged over several hours will be similar for earth stations located tens of kilometers apart (8:2-2). Convective storms are localized and generally produce non-uniform distributions of rainfall and rain rate for a given storm. The total rainfall and rain rate varies significantly over a distance of 10 km (8:2-2).

There are several proposed models for modeling the rainfall attenuation effects on satellite communications.

However, all of these models contain frequency dependent coefficients and require the rain rate statistics for the particular earth station sites since the rain rates vary with location. Currently, rain rate statistics are developed by data collection experiments at the desired location.

Receiver Noise

In addition to the external noise collected by the antenna, noise is also generated within the components of the receiver immediately following the antenna. The contributions from these sources of interference combine to define a total noise level for the receiving system. This noise level set the minimal required power from the desire transmitter to achieve reliable communications.

Noise Temperature. The amount of receiver noise present is defined by the receiver noise temperature, T°_{eq} . This parameter is an effective equivalent temperature that an external noise source would need to produce to have the same amount of receiver noise (11:101).

$$T^{\circ}_{eq} = T^{\circ}_b + (F-1) 290^{\circ} \quad (2.10)$$

where

T°_b = background noise temperature accounting for contributions collected by the antenna from external sources

F = noise figure of receiver

A noise source of temperature T°_{eq} produces an effective noise spectrum level at the antenna input of

$$N_o = KT^o_{eq} \text{ Watts/Hz} \quad (2.11)$$

where

$$\begin{aligned} K &= \text{Boltzmann's constant} = 1.379 \times 10^{-23} \text{ W/K-Hz} \\ &= -228.6 \text{ dBW/K-Hz} \end{aligned}$$

The total noise entering the receiver over a bandwidth, B_{RF} , is

$$P_n = KT^o_{eq} B_{RF} \quad (2.12)$$

where

B_{RF} = bandwidth of the receiver

Therefore, the total receiver noise can be calculated from the knowledge of the T^o_{eq} of the receiver.

Noise Figure. The internal thermal noise is accounted for in T^o_{eq} by specifying the receiver noise figure, F , which depends on the specific electronic circuit components following the antenna. The noise figure for an electronic system is defined as

$$F = \frac{\text{Total system output noise power}}{\text{Output system noise power due to system input noise at } 290^\circ\text{K}} \quad (2.13)$$

When defined as this, $(F-1) 290^\circ\text{K}$ is the temperature of an equivalent noise source at the system input that produces the same contribution to the system output noise as the internal noise of the system itself (11:103). For an example on the specifics on calculating F , see Ziemer and Tranter (23:478-81).

Carrier-To-Noise Ratios (CNR)

One of the most useful indicators of the performance of a communications receiver is the ratio of the received carrier power to the total noise power of the receiver. This RF carrier-to-noise ratio (CNR) is defined as:

$$\text{CNR} = \frac{P_r}{P_n} \quad (2.14)$$

where

$$P_r = (\text{EIRP})L_p L_a G_r$$

$$P_n = K T^\circ_{\text{eq}} B_{\text{eq}}$$

The CNR indicates the relative strength of the desired transmitter-receiver power and the total noise interference (11:104). Eq (2.14) shows how the different link parameters affect receiver CNR. Since the receiver bandwidth B_{RF} is often dependent on the modulation scheme, it is convenient to isolate the RF link power parameters by normalizing the CNR with respect to bandwidth. The resulting RF carrier-to-noise level ratio is defined as

$$(C/N_o) = (\text{EIRP})L_p L_a G_r \quad (2.15)$$

Obviously (C/N_o) is now independent of B_{RF} . In a digital communications system, the (C/N_o) ratio allows us to compute directly the receiver bit energy-to-noise level ratio as

$$E_b/N_o = (C/N_o)T_b \quad (2.16)$$

where

$$T_b = \text{bit time}$$

By knowing the link (C/N_0) , which depends only on the RF link parameters, we can compute the analog CNR by dividing by B_{RF} or the digital E_b/N_0 by multiplying by the bit time. It is convenient to express Eq (2.15) as

$$(C/N_0) = (EIRP/K) (L_p L_a) (G_r/T^o_{eq}) \quad (2.17)$$

where

$(EIRP/K)$ = transmitter parameter

$(L_p L_a)$ = propagation parameter

(G_r/T^o_{eq}) = receiver parameter

Thus, each subsystem of the link contributes to the overall (C/N_0) . The only effect of the receiving system is the ratio G_r/T^o_{eq} . Therefore, as far as the receiver is concerned, performance can be maintained with a lower receiver gain (smaller antenna) if T^o_{eq} (noise) can be reduced. There is a direct trade-off of receiver antenna size and receiver noise temperature in achieving a desired performance.

Power Link Equations

It is convenient to distinguish between the uplink and downlink transmission paths and their corresponding RF carrier-to-noise level ratios. The uplink equation can be described as

$$(C/N_0)_u = EIRP_e - L_{pu} + G_r - T - K - L_{au} \text{ dB-Hz} \quad (2.18)$$

where

$EIRP_e$ = earth station EIRP, dBW

L_{pu} = free space path loss, uplink, dB

G_r = gain of the satellite receive antenna, dBi

T = satellite receiver noise temperature, dB-K

K = Boltzmann's constant = -228.6 dBW/K-Hz

L_{au} = uplink atmospheric losses, dB

The downlink equation is described as

$$(C/N_0)_u = EIRP_s - B0_o - L_{pd} + G_r - T - K - L_{ad} \quad (2.19)$$

dB-Hz

where

$EIRP_s$ = satellite station EIRP, dBW

$B0_o$ = output backoff, dB

L_{pd} = free space path loss, downlink, dB

G_r = gain of the earth station receive antenna, dBi

T = earth station receiver noise temperature, dB-K

K = Boltzmann's constant = -228.6 dBW/K-Hz

L_{ad} = downlink atmospheric losses, dB

Note: The output backoff term is expressed in dB from the saturated output point relative to saturated power. Since the power transfer function is nonlinear for the satellite transponder, $B0_o$ is a nonlinear function (2:14).

Digital Signaling Methods for Satellite Communications Systems

In modern satellite communications systems, the trend has been towards digital instead of analog communications. A digital communication system transmits information waveforms that are first converted into a sequence of data symbols which are then transmitted over the satellite link by encoding onto RF carriers, (11:34), as depicted in Figure 2.1. A major advantage of digital communications is that information can be transmitted relatively error-free with less carrier power than is required for an analog system. For satellite systems, digital communications has the additional advantage that transmitted carrier waveforms can be carefully controlled in terms of amplitudes and frequency spectra, simplifying satellite hardware design (11:34).

The digital information to be transmitted over the channel is assumed to be a sequence of data symbols occurring at a uniform rate of R symbols/second. For binary signaling, the set of data symbols is restricted to a "1" bit and a "0" bit and each symbol may be transmitted directly by sending a waveform corresponding to a "1" or a waveform corresponding to a "0".

As an alternative to transmitting the binary bits directly, the information sequence can be grouped into blocks, where each block consists of k bits (19:140). With k bits/block, there are $2^k = M$ distinct blocks. Therefore, M different waveforms are needed to transmit the k -bit blocks unambiguously.

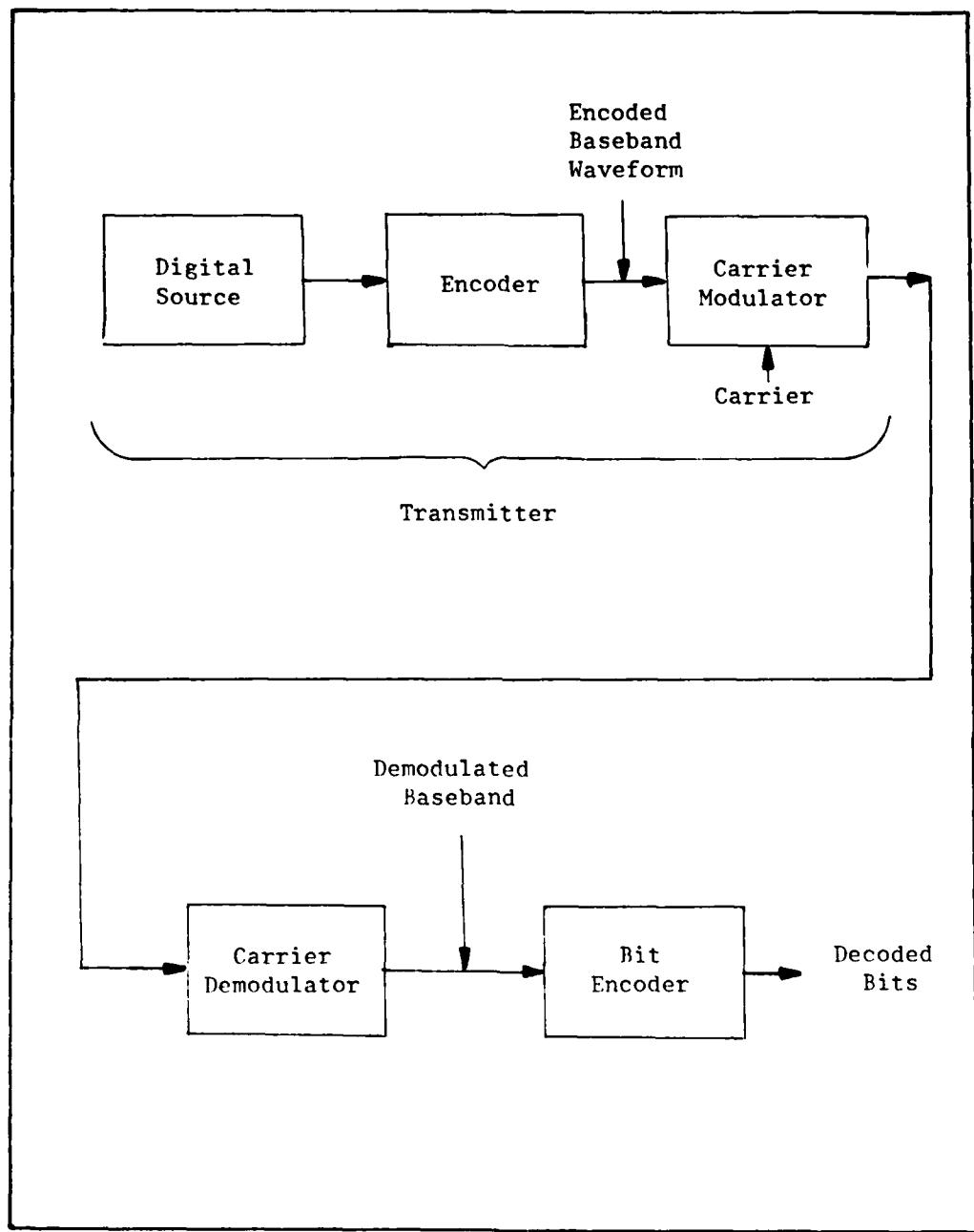


Figure 2.1 Digital Communications Block Diagram

Source: (11:35)

The commonly used measure of performance for digital communications systems is the relationship between bit error rate and signal-to-noise ratio (SNR) (2:38). The SNR for digital systems is usually expressed as the ratio energy per bit to the noise spectral density (E_b/N_o). Generally, the desired modulation technique will be the one that satisfies the required system constraints and requires the least value for E_b/N_o for a specified threshold error rate.

Digital systems can be easily compared on the basis of ideal bit error rate. In comparing digital satellite communications systems the ideal bit error rate is used to determine the best possible performance. The following assumptions are made for the "ideal bit error rate" conditions (2:39):

1. No phase or frequency uncertainties are introduced by earth station or satellite oscillators.
2. No forward error correcting codes are used.
3. Carrier and clock recovery is perfect, so that there is no recovered carrier phase or clock jitter.
4. The only source of errors is the addition of random additive white gaussian noise by the channel.

Multiphase Signaling Waveforms. In a general M-ary signaling system, the possible transmitted signal waveforms may be denoted as $\{s_m(t)\}, m = 1, 2, \dots, M$. We shall consider these waveforms to be bandpass signals, and represent them as

$$s_m(t) = \operatorname{Re}[U_m(t)\exp(j\pi f_c t)] \quad (2.20)$$

where

$$m = 1, 2, \dots, M$$

$\{u_m(t)\}$ = the equivalent low-pass waveforms

Re = the real part of

The M signals are characterized individually by their energy, defined as,

$$\begin{aligned} \mathcal{E}_m &= \int_0^T s_m^2(t) dt \\ &= 0.5 \int_0^T |u_m(t)|^2 dt \end{aligned} \quad (2.21)$$

where

$$m = 1, 2, \dots, M$$

Note: We shall assume that all M signaling waveforms have equal energy such that

$$\mathcal{E} = \mathcal{E}_m \quad (2.22)$$

where

$$m = 1, 2, \dots, M$$

For M -ary phase shift keying (PSK), the baseband signaling waveforms $\{s_m(t)\}$ are used to phase modulate the RF carrier. The general representation for a set of M -ary phase signaling waveforms is

$$s_m(t) = Re\{u(t) \exp j(2\pi f_c t + (2\pi(m-1)/M) + \lambda)\} \quad (2.23)$$

where

$$m = 1, 2, \dots, M$$

$$0 < t < T$$

λ is a fixed initial phase

If $u(t) = A, 0 < t < T$

and

$u(t) = 0, \text{ otherwise}$

then $s_m(t)$ may be expressed as a PSK signal

$$s_m(t) = A \cos[2\pi f_c t + (2\pi(m-1)/M) + \lambda] \quad (2.24)$$

where

$$m = 1, 2, \dots, M$$

$$0 < t < T$$

Performance of M-ary PSK. The probability of bit/symbol error analysis is thoroughly presented in Proakis, (Ref 19, Chap 4). The results of this analysis are:

Case 1: $M = 2$, PSK Waveforms = Antipodal Waveforms

$$P_b = Q[(2\gamma_b)^{0.5}] \quad (2.25)$$

where

P_b = probability of bit error

$\gamma_b = E_b/N_0$ = SNR per bit

$$Q(x) = 1 - \int_{-\infty}^x (1/(2\pi)^{0.5}) \exp(-B^2/2) dB \quad (2.25.a)$$

Case 2: $M = 4, \lambda = \pi/4$

$$P_m = 2Q[(2\gamma_b)^{0.5}] - [Q(2\gamma_b)^{0.5}]^2 \quad (2.26)$$

where

P_m = probability of k-bit symbol error

Case 3: For $M \geq 8$ and $\gamma_b \geq 10$ dB

$$P_m = 2Q((2K\gamma_b)^{0.5} \sin(\pi/M)) \quad (2.27)$$

$$P_b = P_m/k \quad (2.28)$$

Differentially Encoded PSK (DPSK). Ordinary PSK requires coherent processing and accuracy constraints on estimating the phase increase as M increases. A procedure which allows for easier phase and symbol synchronization is called differential PSK. In M -ary DPSK, instead of transmitting signals with phases corresponding to the M possible k -tuples, we transmit phases corresponding to the change (difference) between the previous k -tuple and the current k -tuple (4:V-65).

Performance of DPSK.

For $M = 2$:

$$P_b = 0.5 \exp(-\gamma_b) \quad (2.29)$$

For $M = 4$:

$$P_b = Q(a, b) - 0.5 I_0(ab) \exp[0.5(a^2 + b^2)] \quad (2.30)$$

where

$$Q(a, b) = \exp[0.5(a^2 + b^2)] \sum_{K=0}^{\infty} (a/b)^K I_K(ab), \text{ for } b > a > 0$$

$$I_{\alpha}(x) = \sum_{K=0}^{\infty} \frac{(x/2)^{\alpha + 2K}}{K! \Gamma(\alpha + K + 1)}, \quad x \geq 0$$

$$a = 1.0824 (0.5\gamma_b)^{0.5}$$

$$b = 2.6131 (0.5\gamma_b)^{0.5}$$

III. Rainfall Characteristics

Rainfall has a significant effect on satellite communications at frequencies above 10 GHz. Due to the scattering effect by rain which causes attenuation, depolarization, and interference, the characteristics of rain became an important parameter to satellite communications systems designers. In order to understand and appreciate the problem of rainfall attenuation, it is vital to discuss the basic characteristics of rain and its associated statistics.

Rainfall Physical Structure Characteristics

The variability of rain with respect to space and time has been documented as early as the 1950's (1:369). Measurements on the ground have shown that differences in rainfall intensities can occur within distances of a few hundred feet. The understanding of the formation and distribution of large raindrops and high rainfall rates is of great importance to the designers of communications satellite systems.

Heavy rain usually occurs with cellular structures of limited horizontal and vertical extent (1:369). An important characteristic of raincells is their tendency to form into groups of cells within a region called a small mesoscale area which can be $100-400 \text{ km}^2$. As many as seven cells have been observed in a small mesoscale area and up to six small mesoscales areas within a large mesoscale area which is about 1000 km^2 . The variations of the cell distribution with a

mesoscale structure are not purely random; the form of the mesoscale pattern can be greatly influenced by local climatological, meteorological, or topographical effects (1:369). The lifetime of rain showers and thunderstorms is longer than those of an individual cell; however, the lifetime of a single cell can vary greatly from as little as a few minutes to as long as several hours. The dynamics of raincells appear to fall into two basic categories: those in which the rainfall intensity within the cell is well preserved over periods of minutes while the cell itself moves across the terrain, and those in which the cells are basically stationary but exhibit large fluctuations in rainfall intensity with time (1:369).

Rain Rates

Rain is normally measured as the rate (mm/hr) at which the rainfall is collected by a horizontal surface near the ground at the location of interest. Therefore, in order to obtain the rain rate of a particular location, an experiment designed to obtain these statistics must be performed at that location. Since rain varies greatly with time, the raw data contains too much information to be useful, thus the data is processed to reveal the long-term statistical characteristics of rain. The most important of these is the cumulative distribution function (CDF) (10:199), which shows the fraction of time a certain rain rate is not exceeded (see Figure 3.1).

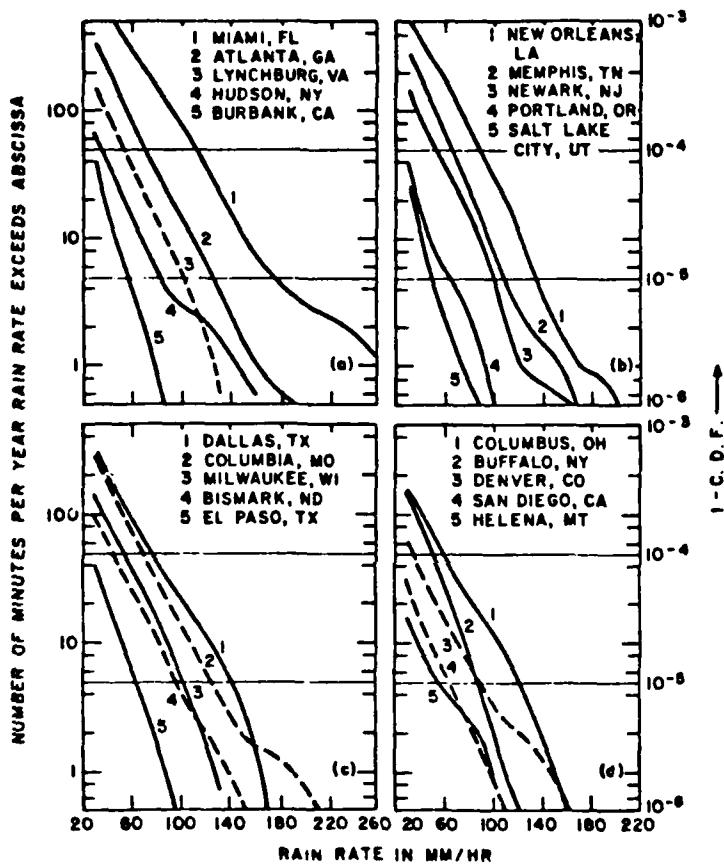


Figure 3.1 Cumulative Distribution Function (C.D.F.) of Rain Rates for 20 U.S. Locations During the Period 1966 to 1970; Based on One-Minute Intervals

Source: (10:200)

In addition, for each rain rate, a typical distribution of drop sizes in a volume of space above and near the rain gauge can be determined as a function of the observed instantaneous rain rate (10:193). Although several rainfall distributions have been developed, some of the more common average dropsize distributions used in rain attenuation calculations are (19:321):

1. Laws and Parsons Distribution: This tabular distribution has been found to be a reasonable measure for an average dropsize spectrum in continental temperate rainfall. It is probably the most widely used distribution currently available.

2. Marshall-Palmer Distribution: This negative exponential distribution is a fairly good fit for the average dropsize spectrum. It is most applicable to the widespread rain in continental temperate climates although it has a tendency to overestimate the number of small drops.

3. "Thunderstorm" Distribution of Joss et. al.: This negative exponential distribution was fitted to the average dropsize spectrum measured in convective rain.

4. "Drizzle" Distribution of Joss et. al.: This negative exponential distribution was obtained by fitting the average dropsize spectrum of very light widespread rain composed mostly of small drops.

A typical Laws and Parsons dropsize distribution of raindrop diameters and velocities for various rain rates is shown in Table 3.1.

TABLE 3.1
Measured Raindrop Terminal Velocities and Dropsize Distributions at Ground Level

Drop Diameter (cm)	Rain Rate (mm/hour)						Terminal Velocity ($\frac{m}{sec}$)			
	0.25	1.25	2.5	5	12.5	25				
	Percent of Total Volume									
0.05	28.0	10.9	7.3	4.7	2.6	1.7	1.2	1.0	1.0	2.1
0.1	50.1	37.1	27.8	20.3	11.5	7.6	5.4	4.6	4.1	3.9
0.15	18.2	31.3	32.8	31.0	24.5	18.4	12.5	8.8	7.6	5.3
0.2	3.0	13.5	19.0	22.2	25.4	23.9	19.9	13.9	11.7	6.4
0.25	0.7	4.9	7.9	11.8	17.3	19.9	20.9	17.1	13.9	7.3
0.3		1.5	3.3	5.7	10.1	12.8	15.6	18.4	17.7	7.9
0.35		0.6	1.1	2.5	4.3	8.2	10.9	15.0	16.1	8.35
0.4		0.2	0.6	1.0	2.3	3.5	6.7	9.0	11.9	8.70
0.45			0.2	0.5	1.2	2.1	3.3	5.8	7.7	9.0
0.5				0.3	0.6	1.1	1.8	3.0	3.6	9.2
0.55					0.2	0.5	1.1	1.7	2.2	9.35
0.6						0.3	0.5	1.0	1.2	9.5
0.65							0.2	0.7	1.0	9.6
0.7								0.3		

Rain Scattering

In order to calculate a specific attenuation factor that corresponds to a specific rain rate, one must understand the phenomena of rain scattering. When rain particles enter the path of the satellite communications downlink signal, the particles both absorb and scatter the radiation associated with the transmitted signal. The interaction between the rain particles and the electromagnetic field associated with the signal can be satisfactorily computed by using electromagnetic scattering theory. However, exact solutions for the scattering problem are only available for simple shapes and distributions of the dielectric properties of the scatterer within the scatterer (7:176). Rain attenuation may be reasonably modeled using spheres with the assumptions that water is a homogeneous lossy dielectric, the drops are randomly distributed with a volume in accordance with a Poisson process, and the drop size distribution is known (6:460). More complex models of raindrops have been developed to account for the nonspherical physical description of rain but these models have only been partially successful and only at lower rain rates (7:176).

Rain Attenuation Models

The most fundamental quantity in the calculation of rain attenuation statistics for space-earth paths is the attenuation per unit distance, A . There are two general approaches commonly used to calculate A , a theoretical technique and an

empirical method based upon the approximate relationship between A and the rain rate R. Both methods rely on the solution of the scattering problem by Mie (17:377, 7:176, 18:318-9). The validity of the theoretical approach is well established (18:318) and its calculations have been conducted for a wide variety of frequencies. However, the complexity of this approach makes it unsuitable for use by satellite communications systems designers.

The theoretical analysis of the rain attenuation results in the expression

$$A = 4.343 \int_0^{\infty} Q_t(D) N(D) dD \quad (3.1)$$

where

$$Q_t = (4\pi/k^2) \operatorname{Re}[S(0,D)]$$

$S(0,D)$ = forward scattering amplitude

$N(D) dD$ = number density of raindrops with equivalent diameter D in the interval dD

Although it was believed that this equation included only the effects of single scattering, it also included the effects of all the forward multiple scattering processes (i.e., those processes which all paths between scatterers have components in the forward direction) (18:319). As suggested by Hogg and Chu (14:1310-2), these are the only multiple scattering processes which significantly contribute to the coherent rain attenuation.

The second method of calculating the rain attenuation is based on the approximation

$$A = aR^b \quad (3.2)$$

where

a, b = functions of frequency, raindrop size distribution, and rain temperature

This expression serves as a good approximation for the full Mie solution obtained in the theoretical approach for frequencies greater than 1 GHz and is suitable for most design applications. The difficulty with this method is obtaining accurate values for the coefficients a and b . Many methods for obtaining the coefficients have been developed including linear ($b=1$) and nonlinear relations, values for the coefficients at different frequencies by fitting the results of Mie calculations, and experimentally obtained empirical values for a and b (18:318). As expected, there are minor discrepancies in the values for these coefficients. An often used set of coefficient values is presented by Olsen, Rogers, and Hodges (18). This method presents a complete set of values of a and b for frequencies 1-1000 GHz where the values of specific attenuation obtained at several rain rates were used to determine a and b by means of logarithmic regression for different combinations of frequency, dropsize distribution, and temperature (See Tables 3.2, 3.3, 3.4).

Statistical Behavior of Rain

In addition to the models to calculate a rain attenuation factor, there has been attempts to characterize the behavior of rain attenuation. One such effort is the work by

TABLE 3.2

Regression Calculations For a and b in
 $A = aR^b$ (dB/km) as Functions of Frequency
 and Dropsize Distribution with Rain Temperature = 20°C

FREQ. (GHz)	a					b				
	LP _L	LP _H	WP	J-T	J-D	LP _L	LP _H	WP	J-T	J-D
1.0	3.04x10 ⁻⁵	3.17x10 ⁻⁵	5.14x10 ⁻⁵	2.02x10 ⁻⁵	5.17x10 ⁻⁵	0.889	0.945	0.852	0.896	0.843
1.5	0.52x10 ⁻⁴	6.75x10 ⁻⁵	1.14x10 ⁻⁴	5.53x10 ⁻⁵	1.14x10 ⁻⁴	0.905	0.972	0.867	0.960	0.846
2.0	1.53x10 ⁻⁴	1.15x10 ⁻⁴	2.02x10 ⁻⁴	7.82x10 ⁻⁵	2.03x10 ⁻⁴	0.926	1.007	0.887	1.065	0.850
2.5	2.42x10 ⁻⁴	1.73x10 ⁻⁴	3.19x10 ⁻⁴	8.29x10 ⁻⁵	3.20x10 ⁻⁴	0.951	1.049	0.913	1.234	0.856
3.0	3.57x10 ⁻⁴	2.39x10 ⁻⁴	4.64x10 ⁻⁴	1.01x10 ⁻⁴	4.67x10 ⁻⁴	0.980	1.096	0.943	1.357	0.863
3.5	4.99x10 ⁻⁴	3.11x10 ⁻⁴	6.40x10 ⁻⁴	1.01x10 ⁻⁴	6.46x10 ⁻⁴	1.013	1.151	0.981	1.533	0.870
4.0	6.73x10 ⁻⁴	3.78x10 ⁻⁴	8.46x10 ⁻⁴	2.45x10 ⁻⁴	8.59x10 ⁻⁴	1.052	1.219	1.025	1.451	0.878
5.0	1.12x10 ⁻³	5.15x10 ⁻⁴	1.38x10 ⁻³	7.49x10 ⁻⁴	1.40x10 ⁻³	1.150	1.377	1.122	1.414	0.896
6.0	1.79x10 ⁻³	1.06x10 ⁻³	2.13x10 ⁻³	2.17x10 ⁻³	2.13x10 ⁻³	1.238	1.393	1.209	1.305	0.921
7.0	2.82x10 ⁻³	2.04x10 ⁻³	3.26x10 ⁻³	4.59x10 ⁻³	3.06x10 ⁻³	1.284	1.380	1.255	1.236	0.945
8.0	4.34x10 ⁻³	3.78x10 ⁻³	4.84x10 ⁻³	1.01x10 ⁻²	4.25x10 ⁻³	1.299	1.342	1.280	1.114	0.972
9.0	6.44x10 ⁻³	6.74x10 ⁻³	7.10x10 ⁻³	1.55x10 ⁻²	5.73x10 ⁻³	1.296	1.285	1.274	1.076	0.998
10	9.20x10 ⁻³	1.11x10 ⁻²	1.01x10 ⁻²	1.90x10 ⁻²	7.52x10 ⁻³	1.280	1.229	1.260	1.079	1.024
11	1.27x10 ⁻²	1.67x10 ⁻²	1.37x10 ⁻²	2.42x10 ⁻²	9.67x10 ⁻³	1.259	1.181	1.244	1.060	1.047
12	1.68x10 ⁻²	2.33x10 ⁻²	1.81x10 ⁻²	3.25x10 ⁻²	3.22x10 ⁻²	1.236	1.142	1.223	1.022	1.067
15	3.28x10 ⁻²	4.59x10 ⁻²	3.57x10 ⁻²	5.89x10 ⁻²	2.20x10 ⁻²	1.173	1.176	1.160	0.966	1.106
20	6.83x10 ⁻²	8.59x10 ⁻²	7.51x10 ⁻²	0.103	6.56x10 ⁻²	1.111	1.044	1.103	0.934	1.123
25	0.113	0.143	0.127	0.181	7.76x10 ⁻²	1.075	1.007	1.064	0.868	1.119
30	0.168	0.228	0.191	0.273	0.118	1.048	0.955	1.032	0.816	1.113
35	0.235	0.337	0.269	0.360	0.167	1.009	0.904	0.999	0.782	1.107
40	0.312	0.452	0.360	0.439	0.225	0.972	0.864	0.866	0.757	1.101
50	0.484	0.648	0.572	0.610	0.368	0.901	0.815	0.900	0.708	1.082
60	0.652	0.775	0.796	0.771	0.541	0.845	0.794	0.847	0.667	1.055
70	0.802	0.850	1.01	0.814	0.735	0.803	0.785	0.807	0.663	1.020
80	0.934	0.902	1.21	0.810	0.936	0.771	0.780	0.772	0.671	0.985
90	1.03	0.938	1.39	0.876	1.14	0.751	0.776	0.744	0.656	0.952
100	1.09	0.958	1.53	0.995	1.33	0.738	0.774	0.721	0.627	0.920
110	1.13	0.972	1.64	1.09	1.50	0.729	0.772	0.705	0.608	0.891
120	1.17	0.982	1.74	1.11	1.66	0.721	0.771	0.693	0.599	0.865
150	1.33	1.02	1.96	1.02	2.05	0.692	0.768	0.667	0.615	0.807
200	1.50	1.06	2.09	0.993	2.47	0.664	0.764	0.644	0.617	0.748
250	1.46	1.02	2.17	0.991	2.69	0.664	0.765	0.626	0.613	0.703
300	1.41	0.993	2.24	0.997	2.84	0.665	0.765	0.612	0.607	0.679
350	1.40	0.980	2.22	0.981	2.92	0.664	0.765	0.612	0.607	0.666
400	1.36	0.958	2.18	0.959	2.95	0.665	0.766	0.613	0.609	0.659
500	1.31	0.976	2.14	0.937	2.97	0.668	0.768	0.612	0.609	0.641
600	1.27	0.902	2.11	0.917	2.98	0.670	0.758	0.610	0.609	0.623
700	1.25	0.886	2.08	0.897	2.96	0.671	0.769	0.610	0.611	0.617
800	1.23	0.871	2.05	0.881	2.94	0.672	0.770	0.610	0.612	0.615
900	1.21	0.861	2.03	0.867	2.91	0.673	0.770	0.610	0.614	0.613
1000	1.20	0.851	2.01	0.856	2.89	0.674	0.770	0.610	0.615	0.613

Source: (18:323)

TABLE 3.3

Regression Calculations For a and b in
 $A = aR^b$ (dB/km) as Functions of Frequency
 and Dropsize Distribution with Rain Temperature = 0°C

FREQ. (GHz)	a					b				
	LP _L	LP _H	RP	J-T	J-B	LP _L	LP _H	RP	J-T	J-B
1.0	6.41x10 ⁻⁵	5.25x10 ⁻⁵	8.60x10 ⁻⁵	4.71x10 ⁻⁵	8.63x10 ⁻⁵	0.891	0.947	0.853	0.899	0.843
1.5	1.45x10 ⁻⁴	1.14x10 ⁻⁴	1.93x10 ⁻⁴	9.31x10 ⁻⁵	1.94x10 ⁻⁴	0.908	0.976	0.870	0.967	0.847
2.0	2.61x10 ⁻⁴	1.96x10 ⁻⁴	3.45x10 ⁻⁴	1.36x10 ⁻⁴	3.47x10 ⁻⁴	0.930	1.012	0.891	1.069	0.851
2.5	4.16x10 ⁻⁴	2.96x10 ⁻⁴	5.46x10 ⁻⁴	1.63x10 ⁻⁴	5.48x10 ⁻⁴	0.955	1.054	0.917	1.202	0.857
3.0	6.15x10 ⁻⁴	4.12x10 ⁻⁴	7.99x10 ⁻⁴	2.09x10 ⁻⁴	8.01x10 ⁻⁴	0.984	1.100	0.947	1.303	0.864
3.5	8.61x10 ⁻⁴	5.42x10 ⁻⁴	1.11x10 ⁻³	3.08x10 ⁻⁴	1.11x10 ⁻³	1.015	1.150	0.981	1.351	0.871
4.0	1.16x10 ⁻³	6.84x10 ⁻⁴	1.47x10 ⁻³	5.08x10 ⁻⁴	1.48x10 ⁻³	1.049	1.202	1.016	1.350	0.879
5.0	1.94x10 ⁻³	1.12x10 ⁻³	2.41x10 ⁻³	1.38x10 ⁻³	2.40x10 ⁻³	1.113	1.274	1.079	1.268	0.896
6.0	3.05x10 ⁻³	1.99x10 ⁻³	3.71x10 ⁻³	3.06x10 ⁻³	3.59x10 ⁻³	1.158	1.285	1.124	1.221	0.913
7.0	4.55x10 ⁻³	3.36x10 ⁻³	5.44x10 ⁻³	5.57x10 ⁻³	5.07x10 ⁻³	1.180	1.270	1.147	1.167	0.929
8.0	6.49x10 ⁻³	5.35x10 ⁻³	7.65x10 ⁻³	9.07x10 ⁻³	6.86x10 ⁻³	1.187	1.245	1.156	1.118	0.943
9.0	8.85x10 ⁻³	8.03x10 ⁻³	1.04x10 ⁻²	1.29x10 ⁻²	8.96x10 ⁻³	1.185	1.216	1.155	1.091	0.957
10	1.17x10 ⁻²	1.14x10 ⁻²	1.36x10 ⁻²	1.69x10 ⁻²	1.14x10 ⁻²	1.178	1.189	1.150	1.076	0.966
11	1.50x10 ⁻²	1.52x10 ⁻²	1.73x10 ⁻²	2.12x10 ⁻²	1.41x10 ⁻²	1.171	1.167	1.143	1.065	0.977
12	1.86x10 ⁻²	1.96x10 ⁻²	2.15x10 ⁻²	2.62x10 ⁻²	1.72x10 ⁻²	1.162	1.150	1.136	1.052	0.985
15	3.21x10 ⁻²	3.47x10 ⁻²	3.66x10 ⁻²	4.66x10 ⁻²	2.82x10 ⁻²	1.142	1.179	1.118	1.070	1.003
20	6.26x10 ⁻²	7.99x10 ⁻²	7.19x10 ⁻²	9.83x10 ⁻²	5.30x10 ⁻²	1.119	1.083	1.097	0.946	1.020
25	0.305	0.132	0.121	0.173	0.81x10 ⁻²	1.094	1.029	1.074	0.884	1.033
30	0.162	0.226	0.186	0.274	0.128	1.061	0.964	1.043	0.823	1.044
35	0.232	0.345	0.268	0.372	0.180	1.022	0.927	1.007	0.783	1.053
40	0.313	0.467	0.362	0.451	0.241	0.981	0.864	0.972	0.760	1.058
50	0.489	0.669	0.579	0.629	0.387	0.907	0.815	0.905	0.709	1.053
60	0.658	0.796	0.801	0.804	0.558	0.850	0.794	0.851	0.662	1.035
70	0.801	0.869	1.00	0.833	0.740	0.809	0.784	0.812	0.661	1.009
80	0.924	0.913	1.19	0.809	0.922	0.778	0.780	0.781	0.674	0.980
90	1.02	0.945	1.35	0.857	1.10	0.756	0.776	0.753	0.663	0.953
100	1.08	0.966	1.48	0.961	1.26	0.742	0.774	0.730	0.637	0.928
110	1.12	0.979	1.59	1.06	1.41	0.734	0.771	0.714	0.614	0.904
120	1.15	0.981	1.67	1.10	1.55	0.727	0.771	0.702	0.604	0.882
150	1.25	0.993	1.88	1.04	1.89	0.703	0.789	0.677	0.610	0.829
200	1.46	1.05	2.06	1.01	2.33	0.668	0.764	0.648	0.612	0.775
250	1.49	1.04	2.13	0.983	2.60	0.660	0.763	0.634	0.614	0.724
300	1.44	1.00	2.24	0.976	2.78	0.661	0.764	0.614	0.611	0.692
350	1.44	0.990	2.23	0.968	2.87	0.659	0.765	0.610	0.609	0.673
400	1.40	0.969	2.19	0.951	2.92	0.660	0.765	0.611	0.610	0.664
500	1.33	0.930	2.14	0.934	2.94	0.665	0.767	0.611	0.609	0.650
600	1.28	0.902	2.11	0.920	2.96	0.659	0.768	0.609	0.608	0.630
700	1.25	0.884	2.08	0.901	2.96	0.671	0.769	0.610	0.610	0.620
800	1.22	0.868	2.05	0.884	2.94	0.672	0.770	0.610	0.611	0.616
900	1.21	0.858	2.03	0.869	2.91	0.673	0.770	0.610	0.613	0.614
1000	1.19	0.850	2.00	0.856	2.99	0.674	0.771	0.610	0.615	0.612

Source: (18:323)

TABLE 3.4

Regression Calculations For a and b in
 $A = aR^b$ (dB/km) as Functions of Frequency
 and Dropside Distribution with Rain Temperature = -10°C

FREQ. (GHz)	a					b				
	LP _L	LP _H	WP	J-T	J-B	LP _L	LP _H	WP	J-T	J-B
1.0	8.68x10 ⁻⁵	7.13x10 ⁻⁵	1.16x10 ⁻⁴	6.35x10 ⁻⁵	1.17x10 ⁻⁴	0.892	0.948	0.854	0.901	0.043
1.5	3.97x10 ⁻⁴	1.55x10 ⁻⁴	2.62x10 ⁻⁴	1.26x10 ⁻⁴	2.63x10 ⁻⁴	0.909	0.978	0.871	0.970	0.047
2.0	3.55x10 ⁻⁴	2.67x10 ⁻⁴	4.71x10 ⁻⁴	1.89x10 ⁻⁴	4.72x10 ⁻⁴	0.931	1.014	0.892	1.065	0.052
2.5	5.68x10 ⁻⁴	4.05x10 ⁻⁴	7.45x10 ⁻⁴	2.48x10 ⁻⁴	7.47x10 ⁻⁴	0.955	1.053	0.917	1.160	0.056
3.0	8.38x10 ⁻⁴	5.68x10 ⁻⁴	1.09x10 ⁻³	3.38x10 ⁻⁴	1.09x10 ⁻³	0.981	1.094	0.944	1.243	0.064
3.5	1.17x10 ⁻³	7.57x10 ⁻⁴	1.51x10 ⁻³	5.06x10 ⁻⁴	1.51x10 ⁻³	1.008	1.134	0.971	1.271	0.070
4.0	1.57x10 ⁻³	9.80x10 ⁻⁴	2.00x10 ⁻³	7.81x10 ⁻⁴	2.00x10 ⁻³	1.033	1.171	0.998	1.270	0.077
5.0	2.59x10 ⁻³	1.62x10 ⁻³	3.26x10 ⁻³	1.79x10 ⁻³	3.22x10 ⁻³	1.077	1.214	1.041	1.228	0.089
6.0	3.96x10 ⁻³	2.64x10 ⁻³	4.91x10 ⁻³	3.45x10 ⁻³	4.76x10 ⁻³	1.105	1.222	1.068	1.180	0.091
7.0	5.70x10 ⁻³	4.14x10 ⁻³	6.98x10 ⁻³	5.68x10 ⁻³	6.63x10 ⁻³	1.119	1.214	1.083	1.145	0.096
8.0	7.81x10 ⁻³	6.07x10 ⁻³	9.50x10 ⁻³	8.43x10 ⁻³	8.82x10 ⁻³	1.125	1.199	1.090	1.118	0.099
9.0	1.03x10 ⁻²	8.46x10 ⁻³	1.25x10 ⁻²	1.16x10 ⁻²	1.16x10 ⁻²	1.126	1.185	1.092	1.099	0.106
10	1.32x10 ⁻²	1.13x10 ⁻²	1.59x10 ⁻²	1.51x10 ⁻²	1.42x10 ⁻²	1.125	1.171	1.092	1.087	0.112
11	1.64x10 ⁻²	1.45x10 ⁻²	1.97x10 ⁻²	1.91x10 ⁻²	1.74x10 ⁻²	1.124	1.161	1.091	1.077	0.118
12	2.00x10 ⁻²	1.81x10 ⁻²	2.35x10 ⁻²	2.37x10 ⁻²	2.09x10 ⁻²	1.122	1.152	1.090	1.064	0.124
15	3.31x10 ⁻²	3.14x10 ⁻²	3.94x10 ⁻²	4.29x10 ⁻²	3.34x10 ⁻²	1.119	1.135	1.088	1.027	0.154
20	6.37x10 ⁻²	6.68x10 ⁻²	7.50x10 ⁻²	9.73x10 ⁻²	6.09x10 ⁻²	1.111	1.086	1.082	0.951	0.171
25	0.107	0.130	0.126	0.174	0.73x10 ⁻²	1.091	1.037	1.065	0.887	0.198
30	0.165	0.226	0.193	0.276	0.143	1.059	0.969	1.037	0.826	1.004
35	0.236	0.346	0.275	0.376	0.197	1.021	0.910	1.002	0.784	1.016
40	0.316	0.468	0.370	0.455	0.260	0.981	0.867	0.968	0.761	1.026
50	0.487	0.665	0.579	0.619	0.404	0.910	0.818	0.904	0.714	1.027
60	0.645	0.789	0.787	0.800	0.564	0.856	0.796	0.854	0.664	1.016
70	0.777	0.860	0.973	0.840	0.728	0.817	0.785	0.817	0.659	0.997
80	0.888	0.903	1.14	0.808	0.888	0.787	0.761	0.789	0.673	0.974
90	0.980	0.935	1.28	0.834	1.04	0.765	0.777	0.764	0.664	0.953
100	1.05	0.957	1.41	0.920	1.18	0.749	0.774	0.741	0.646	0.933
110	1.09	0.974	1.51	1.01	1.32	0.739	0.771	0.724	0.624	0.914
120	1.12	0.980	1.59	1.06	1.44	0.733	0.770	0.712	0.611	0.896
150	1.20	0.979	1.60	1.05	1.76	0.711	0.769	0.686	0.610	0.846
200	1.42	1.03	2.04	1.02	2.21	0.674	0.765	0.652	0.609	0.754
250	1.50	1.04	2.11	1.01	2.53	0.659	0.763	0.638	0.608	0.739
300	1.45	1.01	2.22	0.972	2.72	0.660	0.764	0.618	0.617	0.704
350	1.45	0.994	2.23	0.963	2.82	0.658	0.764	0.612	0.610	0.684
400	1.42	0.976	2.19	0.942	2.88	0.658	0.765	0.611	0.612	0.669
500	1.34	0.936	2.14	0.927	2.91	0.664	0.767	0.611	0.617	0.655
600	1.29	0.904	2.11	0.919	2.94	0.668	0.768	0.608	0.609	0.634
700	1.25	0.883	2.06	0.903	2.95	0.671	0.769	0.609	0.609	0.622
800	1.22	0.869	2.05	0.886	2.93	0.672	0.770	0.610	0.611	0.617
900	1.21	0.857	2.03	0.871	2.91	0.673	0.770	0.610	0.613	0.614
1000	1.19	0.849	2.00	0.857	2.89	0.674	0.771	0.611	0.613	0.613

Source: (18:324)

Lin (15:557-81) regarding the behavior of rain attenuation.

Lin gathered 31 sets of experimental data on the statistics of microwave rain attenuation at frequencies above 10 GHz in the U.S., England, Japan, Italy, and Canada and proposed many ideas dealing with the statistical behavior of rain attenuation.

The summary of his findings are as follows:

1. the distribution of rain attenuation, $a(t)$, in dB is approximately lognormal within the attenuation range of 1-50 dB.
2. the distribution of the fade duration, $f(A)$, is also approximately lognormal.

Lin's theory on the lognormal behavior of rain attenuation suggests that three parameters which depend on geographic locations determine the distribution of the rain attenuation. These three parameters are:

P_o = probability of rainfall, the expected fraction of time that rain falls at the location of the satellite earth station

σ_a = standard deviation of the attenuation, $a(t)$

α_m = median of the attenuation, $a(t)$

Lin also stated that α_m is frequency dependent and increases almost linearly with the path length because the median rain is usually small and almost uniform over the entire path. σ_a decreases slightly as frequency increases and decreases slightly as the path length increases because of the averaging effect of the propagation volume.

The equation describing the lognormal distribution of rain attenuation is

$$P(\alpha > A) = 0.5(P_o)(0.5 + Q[(\log_{10} A - \mu_a) / (2^{0.5} \sigma_a)]) \quad (3.3)$$

where

P_o = probability of rainfall

σ_a = standard deviation of $\log_{10} \alpha$ during the raining time

$\mu_a = \log_{10} \alpha_m$

= mean value of $\log_{10} \alpha$ during the raining time

Similarly, the distribution of the fade, $f(A)$, is described by

$$P(f(A) > b) = 0.5(0.5 + Q[(\log_{10} b - \mu_f) / (2^{0.5} \sigma_f)]) \quad (3.4)$$

where

μ_f = mean of $\log_{10} f(A)$

σ_f = standard deviation of $\log_{10} [f(A)]$

Due to the significance of rain attenuation to the satellite communications systems designer, an ideal method that would permit an accurate extrapolation of measured rain characteristics to different geographical locations or other time periods is needed. Since detailed measurements of the various important statistics of rainfall exist for only a few locations throughout the world, it would be of great value if these statistics could be accurately applied or converted to other areas, especially those with different climates. However, a

good deterministic theory of rain generation and rainfall has not been developed, therefore it is not possible to apply it to the prediction of localized rain occurrences.

IV. Diversity Techniques For Satellite Communications

With the recent growth of satellite communications, allocations in the higher frequency bands have been required to relieve the congestion in the 8/7 GHz band. One such allocation is the 30/20 GHz band, which is being considered for many government applications (9:1-1). Unfortunately, a severe problem with rain attenuation exists in the 30/20 GHz frequency band (as noted in Sections II and III).

There are many techniques that can be employed to overcome the rain attenuation. In order to overcome the deep fades on the uplink or downlink, satellite transmitters could employ higher power levels or the associated earth station could use a larger antenna (1:369). However, another concept used to combat the effects of rain attenuation is diversity, which is employed to reduce the margin required for rain attenuation. The main concept of diversity is that the probability of an error can be reduced by using two or more received signals to determine the actual transmitted signal instead of one.

Description of Basic Diversity System

There are three basic types of diversity: angle, frequency, and space (or site). The use of angle diversity requires two or more satellites which are separated physically such that the fading on any earth-space path has a low correlation with the fading on other paths (9:3-1)

(See Figure 4.1). Due to the requirement for two satellites, angle diversity is very costly and it has been shown to be not as effective as the other two diversity methods (9:1-2). Frequency diversity requires that the satellite be equipped with two transponders, one operating in a high frequency band and the other in a lower band. When the rain attenuation is minimal the higher band is used and the lower frequency band transponder is used when the rain attenuation becomes significant. Although the fades in the two bands are correlated, the fade depths in the lower frequency band are less than the higher frequency band. Frequency diversity incurs a relatively high cost for the additional satellite transponder but the performance has been rated the highest of the three diversity methods (9:1-2).

However, the focus of this thesis effort is on space diversity techniques that can be used to combat rain attenuation in the downlink of a satellite communications link. The use of site diversity in the downlink requires that two or more earth terminals be physically separated such that the fading on any space-earth path has a low correlation with the fading on other paths (9:2-1). Dual diversity is the most basic type of space diversity but higher orders of diversity may be needed at locations with a history of heavy rains. However, the higher the order of diversity, the more costly the system due to the additional earth stations.

A block diagram of a dual downlink space diversity system is shown in Figure 4.2. Since the diversity equipment

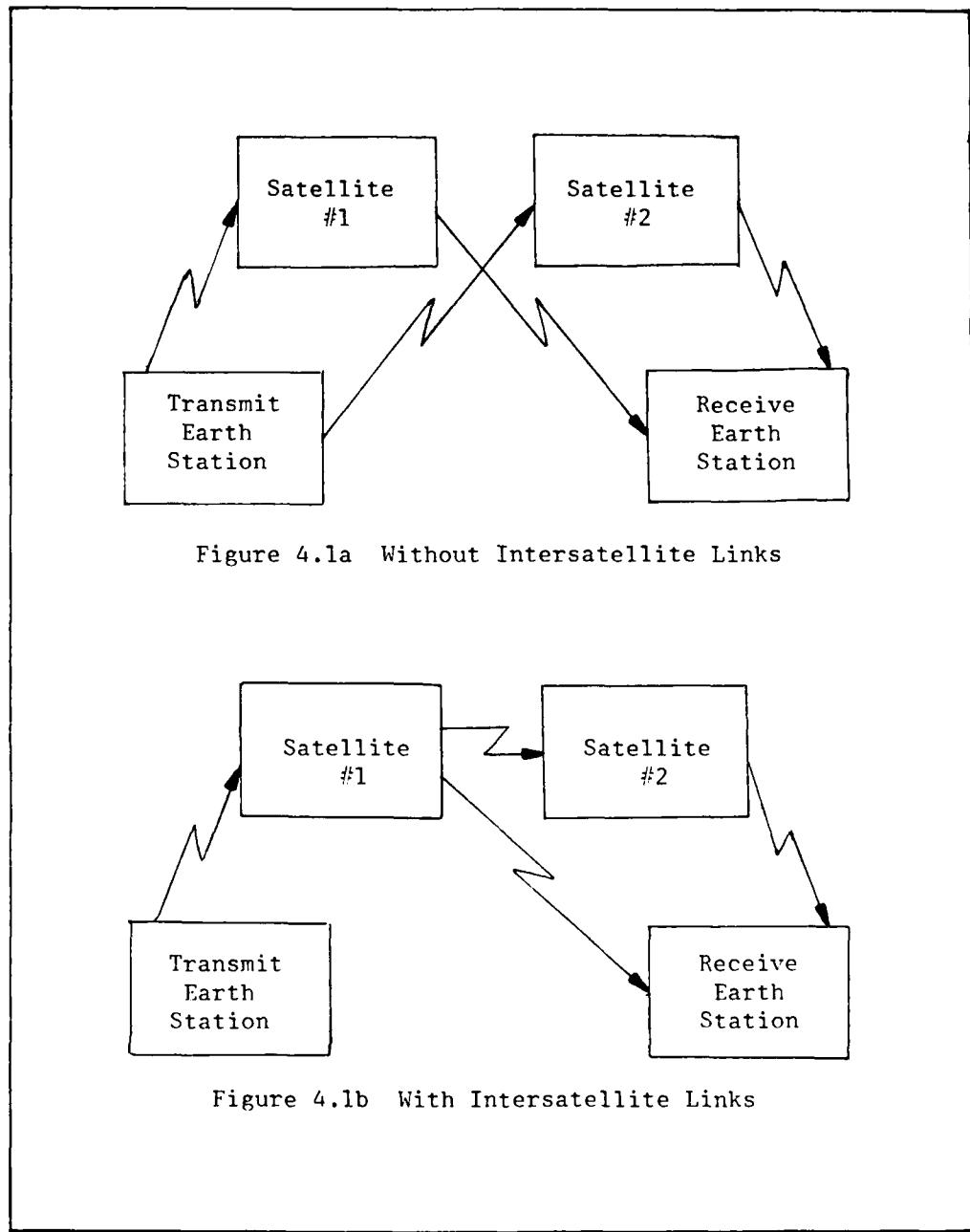


Figure 4.1 Angle Diversity

Source: (9:3-2)

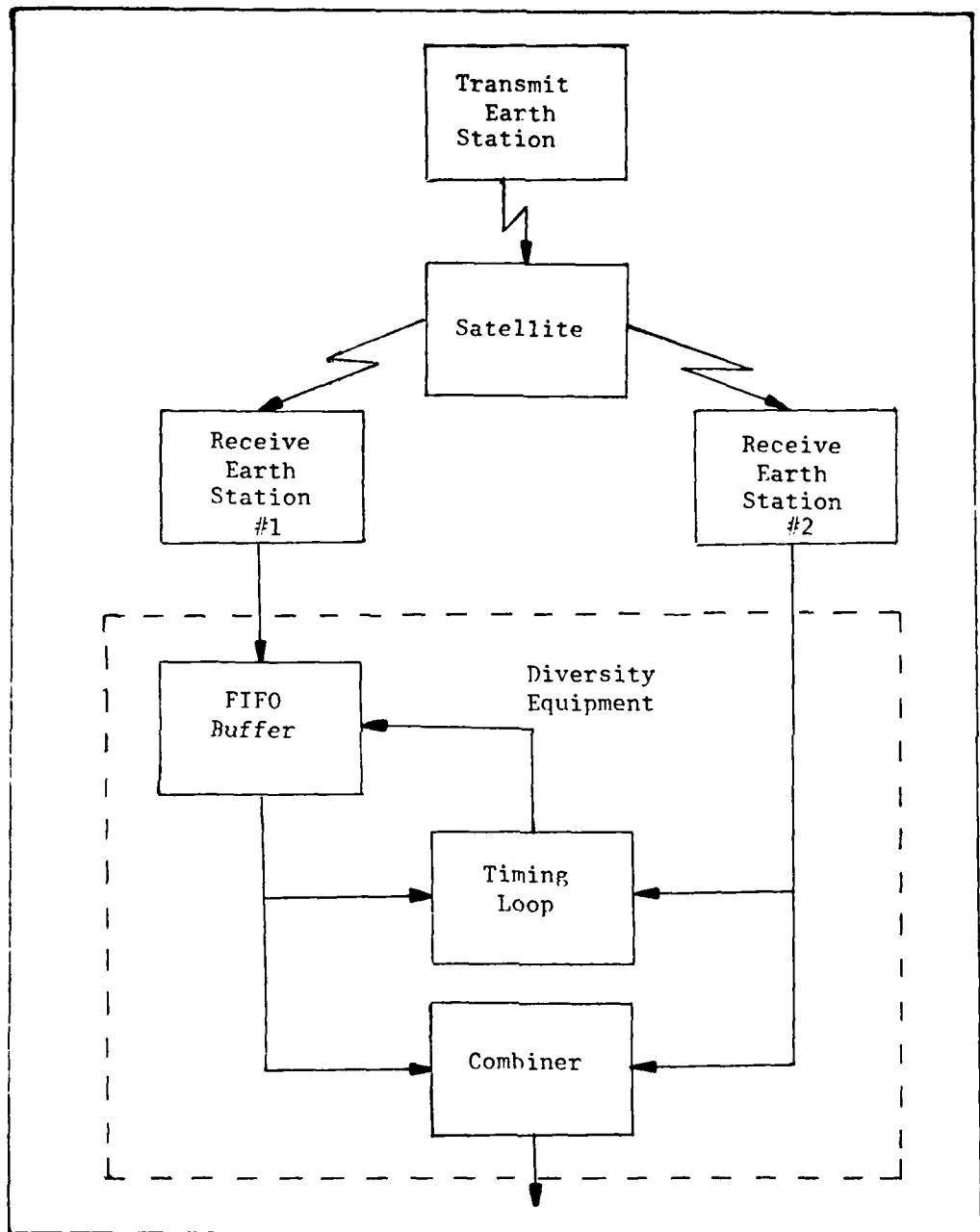


Figure 4.2 Block Diagram--Downlink Space Diversity

combines the digital outputs of the two earth stations, the configuration is independent of whether Frequency Division Multiple Access (FDMA) or Time Division Multiple Access (TDMA) is used on the satellite communications link (9:2-1). The diversity equipment could be collocated with one of the earth stations or it could be located at a separate site.

The optimum spacing between the earth stations is dependent on the characteristics of the rain in that particular area. In practice, optimum spacing may not be achievable because of limitations on the availability of sites for earth stations. However, the spacing will usually be in excess of one mile necessitating the use of a terrestrial link to connect at least one earth station to the diversity equipment.

Bit Stream Synchronization. When using diversity on the downlink, there will usually be a difference in the transmission path lengths from the satellite to the combiner. However, due to the satellite motion, this difference in path lengths will not remain constant. The path length difference and its variation are functions of the relative geographical locations of the earth stations and the satellite (9:2-3). Therefore, due to the path length difference, some adjustment or control must be made to maintain bit synchronization of the bit streams into the combiner. If the path length difference is a significant fraction of a bit, a common practice is to use a first-in-first-out (FIFO) buffer on the shorter path as shown in Figure 4.2 so that the bits arrive

at the combiner in synchronism (9:2-5). If the variation in the path length difference is a significant fraction of a bit, a timing tracking loop is needed to maintain synchronism. In many cases, this loop operates similarly to the code tracking loop in a pseudonoise receiver except that one of the two bit streams is used as a reference (9:2-5).

Linear Diversity Combining Techniques. When using spatial diversity a combining technique must be used to choose the optimum signal from the diversity branches. The most common methods for combining diversity channels outputs are:

1. Selection combining. Selection of the channel with the highest signal level. Measurement of the signal level is required and this method can use either hard or soft decisions.
2. Maximum Selection combining. Selection of the received symbol with the largest amplitude. The method requires soft-decision outputs.
3. Equal Gain. Summing the soft-decision outputs of each channel.
4. Square Law combining. Squaring the soft-decision output of each channel followed by linear summing.
5. Maximum Ratio combining. Weighting the soft-decision output of each channel by the SNR. The measurement of the SNR is required.

The diversity improvement is dependent on many factors including the rain fading characteristics of that particular

area (1:369). However, theoretically, maximum ratio combining is the most efficient, and selection combining is the least (9:2-8). Since the difference in performance between the different combining methods is relatively small, the decision of which method to use can vary with the particular implementation depending on the desired performance criteria and cost restrictions.

Space Diversity Measurements

The rain attenuation effects on the transmitted signal for a slant-path link can be measured directly, or inferred from the measurement of other related parameters by using one of the following techniques (1:369-70):

1. direct reception of a beacon signal transmitted from a geostationary satellite at the required frequency.
2. radiometric measurements using either the sun as a source or the apparent change in sky temperature with rainfall intensity.
3. rapid-response raingauges.
4. radar.

As noted in Table 4.1, there are advantages and limitations for each of the different measurement techniques for obtaining slant-path attenuation. The three major advantages of the radiometer are relative cheapness, extreme reliability and straightforward data reduction. For gathering long-term data for slant-path attenuation, the most cost-effective solution is the radiometer (1:370). Fast-response raingauges,

TABLE 4.1
Measurement Techniques For Obtaining Slant-Path Attenuation

Technique	Relative cost	Elevation angles sampled	Accuracy in calculating attenuation	Comments
(a) Satellite beacon measurements	extremely expensive satellite	fixed	excellent fade margins > 30dB	limited to satellite lifetime
	moderately expensive earth stations			
(b) Radiometers				
(i) sun tracking	moderately cheap	varies with sun	good to 20dB	limited operating hours and elevation angles
(ii) sky-noise Dicke switching	moderately cheap	fixed	good to 13dB	possibly limited to frequencies $\leq 30\text{GHz}$
(iii) sky-noise total power	cheap	fixed	good to 10dB	
(c) Raingauges	very cheap	any	generally poor	highly dependent on wind and rain-drop parameters
(d) Radar	moderate to very expensive	any	variable	highly dependent on physical phase of scattering particles

although inexpensive, do not provide data that can be easily transformed into slant-path attenuation data. In order to provide an accurate transformation of collected data into slant-path attenuation data, an extensive array of rain-gauges, accurate telemetry and large computing facilities are required, which greatly increases the associated costs of this measurement technique. Radar is a very useful tool for investigating propagation phenomena; however, there are also some potential problem areas. Unless great care is used in eliminating all echoes due to solid or solid/liquid phase particles, very large errors will accrue in the calculation of the slant-path attenuation (1:370). The best measurement method for obtaining the desired slant-path propagation data is the satellite beacon technique. However, to orbit radio beacons covering a vast range of frequencies is extremely expensive thus the opportunity of conducting satellite-beacon propagation experiments rarely exists except for a limited period at a few frequencies and locations (1:370).

Diversity Performance Assessment Techniques

There are two major methods currently employed in assessing the performance of space diversity systems: diversity gain and diversity improvement. Diversity gain is defined as the difference between the path attenuation associated with a single earth station and the diversity modes of operation for a given percentage time (13:280). It uses (percentage of) the time as a parameter and expresses the diversity

improvement as the difference in decibels which is the effective increase in fade margin between the single earth station site and the diversity system fading statistics. Diversity improvement is defined as the ratio of the percentage time a given fade depth is exceeded on a single path to the percentage time that the same fade depth is exceeded for the diversity system (13:280). An example of these two performance measures is depicted in Figure 4.3.

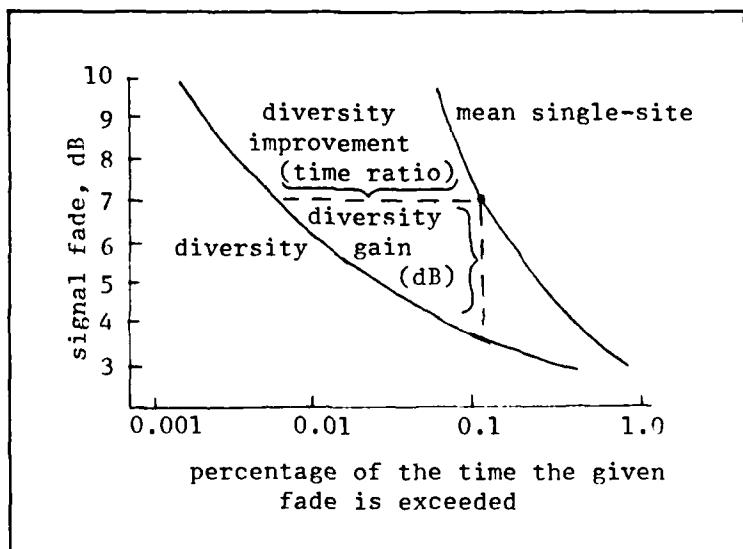


Figure 4.3 Technique for Calculating Diversity Improvement and Diversity Gain from Single-Site and Space Diversity Cumulative Fading Statistics.

Although the methods for describing diversity performance are identical, some space diversity experiments have shown that the diversity gain technique exhibits a more consistent behavior than the diversity improvement technique when different sets of propagation data are compared. This

observation is probably due to the fact that the calculation of the improvement factor involves division by a percentage time which is often very small and therefore subject to considerable uncertainty (13:281). Since diversity gain is a function of the single earth station site fading depth characteristics, it is commonly used to compare sets of space-diversity measurements conducted over different periods of time and during different weather conditions. Hence, the diversity gain method of performance measurement for diversity systems is generally preferred to the diversity improvement method.

Much research has been conducted to develop a model which accurately predicts the performance of a diversity system with respect only to the separation distances between the earth stations and not to the carrier frequency (1,13). One of the best known models of this type is the empirical relationship for path diversity gain developed by D.B. Hodge in the mid-70's (13:280-1). Hodge gathered diversity gain data for millimeter wavelength earth-space propagation paths in Ohio and New Jersey. Although these measurements were collected in different locations and over different time periods, the resulting diversity gain data were very consistent. Hodge used this to develop an empirical relationship for diversity gain as a function of separation distance and single earth station fade depth. He recognized that the diversity gain data followed the same relationship for each

value of the single earth station fade depth. This relationship for diversity gain, G_d , is

$$G_d = a(1 - \exp(-bD)) \quad (4.1)$$

where

$$a = A - 3.6(1 - \exp(-0.24A))$$

$$b = 0.46(1 - \exp(-0.26A))$$

A = single earth station fade depth in dB

D = earth station separation distance in km

The coefficients a and b depend only upon the single earth station fade depth and were found by performing a minimum rms error fit for each fade depth.

Although Hodge's relationship for diversity gain accurately modeled the data measurements collected for his experiment, there have been other similar experiments where the collected data were not accurately modeled by the Hodge relation. Fimbel and Juy assumed that diversity gain was frequency dependent and recalculated the coefficients a and b from Hodge's formula and were able to develop a relationship that more accurately predicted the results of the data measurements that they had collected in the United Kingdom (1:374).

In an effort to improve its accuracy, Hodge later modified his model for diversity gain as a function of earth terminal separation distance, link frequency, elevation angle, and angle between the baseline and the path azimuth (12:1393-9). His new model for diversity gain, G_D , is

$$G_D = G_d G_f G_e G_b \quad (4.2)$$

where

G_d = function defined by Eq (4.1)

G_f = function of frequency

G_e = function of elevation angle

G_b = function of orientation of the baseline relative to the propagation path

$$G_f = 1.64 \exp(-0.025f) \quad (4.3)$$

where f = link frequency in gigahertz

$$G_e = 0.00492e + 0.834 \quad (4.4)$$

where e = elevation angle

$$G_b = 0.00177b + 0.887 \quad (4.5)$$

where b = orientation of the baseline relative to the propagation path in degrees

A set of thirty-four experiments were conducted to validate the Hodge's improved diversity model and the model reproduced the original data set with a rms error of 0.73 dB.

The research in this area has continued but so far no single model developed has been able to accurately predict all of the diversity gain data measurements gathered by experiments conducted throughout the world. It is widely believed that the difficulty in establishing a general model for predicting the diversity gain with respect to separation

distance is that there are several causes of variation for the diversity gain data measurements. The three basic categories which cause diversity gain variation are climatic, geographic, and systemic (1:372).

The climatic factors which cause variations in diversity gain are associated with large scale weather patterns. They are rain lifetimes, rain cell sizes, rain cell separation, and rain cell orientation. In different locations or during different periods, these climatic factors may vary and cause a variation in the diversity gain measurements with respect to earth station separation distances.

The geographic causes relate to the fact that there can be local variations in climate within a limited area as small as 10 km. The geographic feature that seem to enhance or reduce the rainfall-intensity probability at given locations is generally referred to as the microclimate of a region (1:373). These local variations in climate are of particular importance for space diversity communications systems since knowledge of where the high and low probability areas of intense rainfall would greatly aid in the siting of earth stations.

The systemic causes of variations in diversity gain measurements are variation with frequency, variation with elevation angle, variation with baseline orientation, and variation with site separation. The first three variations deal with the concept that rain attenuation varies with frequency and the slant-path of the rain with respect to the

earth station. The fourth variation, separation distance, deals with the fact that a good site location is dependent on several factors, including the microclimate, prevailing wind direction, and the viewing bearing. Thus, the separation distance is dictated by the results of these other factors. However, site separations of approximately 10 km seem to provide diversity gain close to the optimum although some regions will require larger separation distances to achieve the same diversity gain because of geographic and climatic reasons (1:374).

V. Analysis of Selected Linear Diversity Combining Techniques

In the previous section, it was mentioned that a diversity combining technique must be implemented within the diversity network in order to successfully achieve spatial diversity improvements. In this section, some of the diversity combining techniques will be examined so that a probability of bit error analysis can be performed on the selected combinations of diversity techniques and digital signaling schemes. The diversity techniques to be examined are the selection diversity, equal gain, and maximal ratio techniques and the digital signal-schemes are restricted to DQPSK and B-ary PSK. Therefore, the possible combinations of these diversity techniques and signaling schemes will result in six different probability of bit error expressions.

Considerations for Bit Error Analysis

In performing such an analysis, there are assumptions that must be stated in order to validate the analysis. Some of the assumptions for the development of the statistics for the two digital signaling schemes are:

1. The channel through which the signaling waveforms are transmitted is assumed to have no bandwidth restrictions (i.e., the ideal case).
2. The signals transmitted through the channel are corrupted by additive white gaussian noise (AWGN).

3. The receivers at the earth stations are synchronized to the satellite transmitter.

4. The carrier phase is known perfectly at the receiver in order to facilitate ideal coherent demodulation.

5. All of the lowpass signal representations in each particular signaling scheme have the same energy and are equiprobable.

The diversity/signaling scheme combinations will be compared on the basis of average bit error rate, P_B . If

$P_B(\gamma_b)$ = conditional probability of bit error given γ_b for a specified signaling scheme

$p_D(\gamma_b)$ = probability of density function of γ_b for a particular diversity combining technique

then [as in Eq 7.4.14 from (Ref 19:474)]

$$P_B = \int_0^\infty P_B(\gamma_b) p_D(\gamma_b) d\gamma_b \quad (5.1)$$

Consider first DQPSK, Referring to Section II Eq (2.30) of this thesis

$$P_{B,DQPSK}(\gamma_b) = Q(a, b) - 0.5 I_0(a, b) \exp[-0.5(a^2 + b^2)]$$

where

$$a = 1.0824 (0.5\gamma_b)^{0.5}$$

$$b = 2.6131 (0.5\gamma_b)^{0.5}$$

$$Q(a, b) = \exp(-0.5(a^2 + b^2)) \sum_{K=0}^{\infty} \left(\frac{a}{b}\right)^K I_K(ab), \text{ for } b > a > 0$$

A further simplification is provided by Shanmugam
(21:425). For 4-ary DPSK

$$P_{B,DQPSK}(\gamma_b) \approx 2Q\left[\left(4\gamma_b \sin^2(\pi/8)\right)^{0.5}\right] \quad (5.2)$$

For M-ary PSK signaling the probability of a symbol error is expressed by

$$P_M = 1 - \int_{-\frac{\pi}{M}}^{\frac{\pi}{M}} p(\theta) d\theta \quad (5.3)$$

where

$$p(\theta) = \frac{1}{2\pi} \exp(-\gamma_b) \left[1 + \left(4\pi\gamma_b\right)^{0.5} \left(\frac{\cos\theta}{(2\pi)^{0.5}} \right) \right]$$

$$\cdot \exp(\gamma_b \cos^2 \theta) \int_{-\infty}^{\frac{2\gamma_b \cos\theta}{(2\pi)^{0.5}}} \exp(-0.5x^2) dx$$

The probability of a bit error for an 8-ary PSK system with Gray code assignment of 3-tuples (Figure 5.1) can be expressed by

$$P_{B,8PSK}(\gamma_b) = \sum_{K=1}^3 (K \text{ errors}) (P_{eK}) \quad (5.4)$$

where

P_{eK} = probability of error for K bit errors

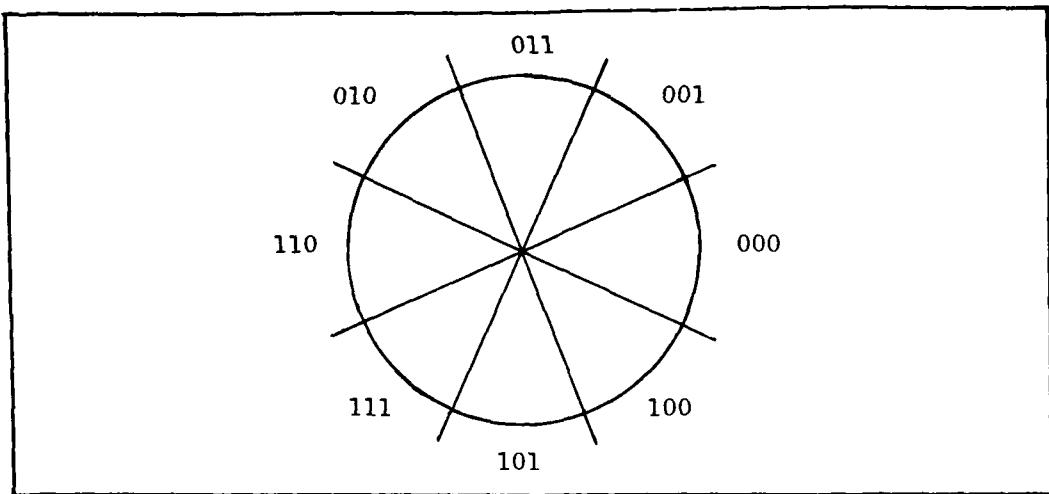


Figure 5.1 Gray Code for 8-ary PSK

Therefore,

$$\begin{aligned}
 P_{B,8PSK}(\gamma_b) = & \left[\int_{\pi/8}^{3\pi/8} p(\theta) d\theta + 2 \int_{3\pi/8}^{5\pi/8} p(\theta) d\theta + \int_{5\pi/8}^{7\pi/8} p(\theta) d\theta \right. \\
 & + 2 \int_{7\pi/8}^{9\pi/8} p(\theta) d\theta + 3 \int_{9\pi/8}^{11\pi/8} p(\theta) d\theta + 2 \int_{11\pi/8}^{13\pi/8} p(\theta) d\theta \\
 & \left. + \int_{13\pi/8}^{15\pi/8} p(\theta) d\theta \right] \quad (5.5)
 \end{aligned}$$

Since $p(\theta)$ is an even function, Eq (5.5) reduces to

$$\begin{aligned}
 P_{B,8PSK}(\gamma_b) = & 2 \int_{\pi/8}^{3\pi/8} p(\theta) d\theta + 4 \int_{3\pi/8}^{5\pi/8} p(\theta) d\theta + 4 \int_{5\pi/8}^{7\pi/8} p(\theta) d\theta \\
 & + \int_{7\pi/8}^{\pi} p(\theta) d\theta \quad (5.6)
 \end{aligned}$$

Due to the complexity of evaluating the substitution of Eq (5.3) into Eq (5.6), the approximation denoted by Eq (2.28) is commonly used for the probability of bit error for high order M-ary PSK systems. For 8-ary PSK

$$P_{B,8PSK}(\gamma_b) \approx \frac{2}{3} Q[(6\gamma_b)^{0.5} \sin(\pi/8)] \quad (5.7)$$

Assumptions for Diversity Analysis

Having developed the probability of bit error for each signaling scheme, we must now look at the different linear diversity techniques. Since the digital signaling techniques being used require coherency, we will limit the diversity techniques to those which are most commonly used with coherent signaling schemes. These three diversity techniques, selection, equal gain, and maximal ratio, can all be generally described by the equation

$$f(t) = a_1 f_1(t) + \dots + a_L f_L(t) = a_j f_j(t) \quad (5.8)$$

where

$f(t)$ = selected output of diversity system

a_j = combining coefficient proportional to the gain of the j th channel

f_j = received signal of the j th channel

L = number of diversity channels

There are several assumptions about the channel characteristics that must be stated before attempting further development. The basic assumptions are made for the channels when employing the selected linear diversity techniques are:

1. The channel impulse response will be modeled as a zero mean complex-valued gaussian process so that its envelope at any time, t , is Rayleigh-distributed.

2. The amplitude variations in the received signal, i.e., signal fading, are caused by the time-variant multi-path channel characteristics. Due to assumption 1, the channel attenuation, α , is Rayleigh-distributed; therefore α^2 has a chi-square probability distribution with 2 degrees of freedom. Since E_b is dependent on α^2 , γ_b is also chi-square-distributed.

3. The information-bearing signal transmitted through the channel is large in comparison to the bandwidth of the transmitted signal so that the channel is considered frequency-nonselective.

4. The signal bandwidth and the signaling interval shall be chosen small enough so that the channel attenuation and phase shift are essentially fixed for the duration of at least one signaling interval; therefore the channel can be considered slowly fading.

5. The channel fading is sufficiently slow so that the phase shift can be perfectly estimated from the received signal.

6. The noise in each channel is independent of the signal and additive; and the received signal, $f_j(t) = s_j(t) + n_j(t)$, where s_j and n_j are the signal and noise components, respectively, in the j th channel.

7. The noise components, $n_j(t)$ are locally uncorrelated and have zero means.

Probability of Error in Rayleigh Channel with No Diversity

In order to evaluate the benefits of a diversity system, the probability of a bit error must be calculated for DQPSK and 8-ary PSK in a frequency-nonselective, slowly Rayleigh fading channel without diversity using the same assumptions about the channels as for the diversity case. By assumption 2, γ_b is chi-square distributed, therefore,

$$P_{\text{no diversity}}(\gamma_b) = \frac{1}{\gamma_b} \exp(-\gamma_b/\bar{\gamma}_b) \quad (5.9)$$

Using Eq (5.1), the probability of a bit error can be obtained for DQPSK and 8-ary PSK in a Rayleigh channel without diversity.

For DQPSK,

$$P_B(\text{DQPSK, no diversity}) = \int_0^{\infty} \frac{1}{\gamma_b} \exp(-\gamma_b/\bar{\gamma}_b) \cdot P_{B, \text{DQPSK}}(\bar{\gamma}_b) d\gamma_b \quad (5.10)$$

where

$$P_{B, \text{DQPSK}}(\bar{\gamma}_b) = 2Q[4\bar{\gamma}_b \sin^2(\pi/8)]^{0.5}$$

For 8-ary PSK,

$$P_B(\text{8PSK, no diversity}) = \int_0^{\infty} \frac{1}{\bar{\gamma}_b} \cdot \exp(-\gamma_b/\bar{\gamma}_b) \cdot P_{B, \text{8PSK}}(\gamma_b) d\gamma_b \quad (5.11)$$

where

$$P_{B,8PSK}(\gamma_b) = \frac{2}{3} Q[(6\gamma_b)^{0.5} \sin(\pi/8)]$$

Selection Diversity

The basic principle of the selection diversity technique is that at any given time, the system picks out the best of the L noisy signals f_1, f_2, \dots, f_L , and uses that one alone; and the other signals do not contribute to $f(t)$ (3:1081). The ideal selection diversity combiner is defined as choosing for the system output, during each "instant" of time, the signal from that receiver which has the largest SNR (See Figure 5.2). Therefore, the parameter used to determine the optimum diversity channel is received SNR. If K denotes the index of a channel for which $E_{bK} > E_{bj}$, $j = 1, 2, \dots, L$; where $j = K$, then this type of system can be characterized by the Eq (5.8) where

$$a_j = \begin{cases} 1, & \text{for } j = K \\ 0, & \text{for } j \neq K \end{cases} \quad (5.12)$$

Several methods can be employed for selecting the optimum diversity channel signal. One of the easiest is if all the receivers have the same noise level then the channel with highest total instantaneous power is selected.

Analysis of Selection Diversity

Given the assumption of short-term fading, the performance of selection diversity can be obtained from the

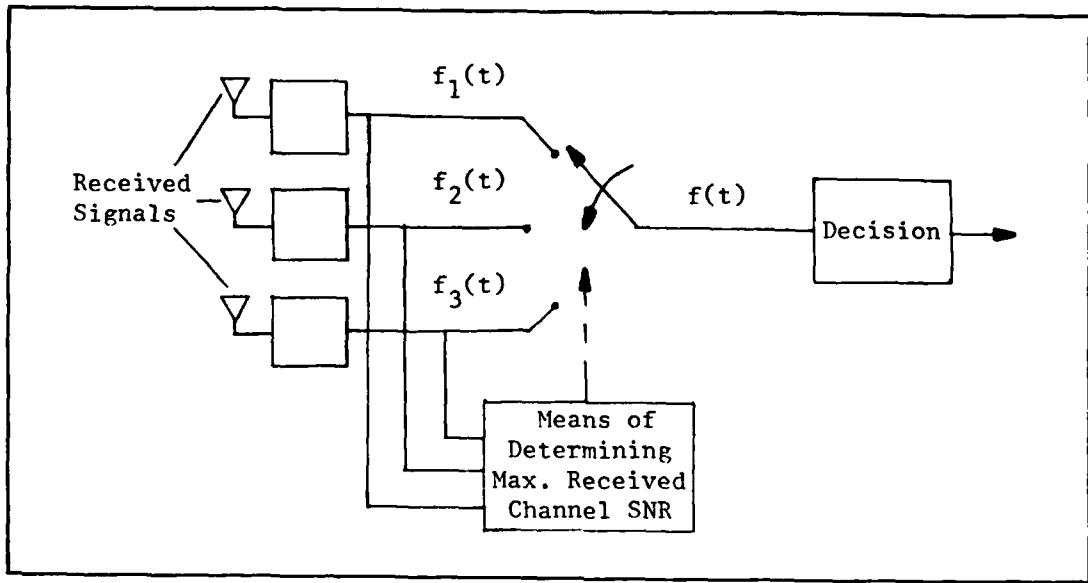


Figure 5.2 Selection Diversity

statistics of the SNR at the selector output. In particular, the p.d.f. of γ_{bK} , the instantaneous SNR in the Kth channel is needed. Following the development of Schwartz, et al., (20:434-5), $p_D(\gamma_{bK})$, can be easily obtained. Assuming Rayleigh fading and defining $\bar{\gamma}_{cK}$ as the average of γ_b over the short-term fading for the Kth channel so that

$$\bar{\gamma}_{cK} = E\{\gamma_{cK}\} = \frac{E\{\alpha_K^2\} \epsilon}{N_K} \quad (5.13)$$

where

α_K = attenuation factor of Kth channel

ϵ = energy of signal transmitted

N_K = power spectral density of Kth channel

yields the individual p.d.f.'s

$$p_D(\gamma_{bK}) = \frac{1}{\bar{\gamma}_{cK}} \exp(-\gamma_{bK}/\bar{\gamma}_{cK}) \quad (5.14)$$

and the associated cumulative distributions are

$$P(\gamma_{bK} < X) = 1 - \exp(-X/\bar{\gamma}_{cK}) \quad (5.15)$$

Over short-term fading, all the events in which the selector output SNR, γ_b , is less than X is exactly the set of events in which each of the channel SNR's is simultaneously below X (20:435). Since the fading is assumed independent in each of the L channels, the probability that $\gamma_b < X$ is the product of the independent probabilities that each $\gamma_{bK} < X$.

Therefore,

$$P(\gamma_b < X) = \prod_{K=1}^L P(\gamma_{bK} < X) = \prod_{K=1}^L [1 - \exp(-X/\bar{\gamma}_{cK})] \quad (5.16)$$

The corresponding p.d.f. for γ_b is

$$p_D(\gamma_b) = \frac{d}{dX} \left\{ \prod_{K=1}^L [1 - \exp(-X/\bar{\gamma}_{cK})] \right\} \Big|_{X=\gamma_b} \quad (5.17)$$

$$= \frac{d}{d\gamma_b} \left\{ \prod_{K=1}^L [1 - \exp(-\gamma_b/\bar{\gamma}_{cK})] \right\} \quad (5.18)$$

If we assume all diversity channels have equal mean SNR over the short-term fading, $\bar{\gamma}_{cK} = \bar{\gamma}_c$; then

$$P(\gamma_b < x) = [1 - \exp(-x/\bar{\gamma}_c)]^L \quad (5.19)$$

$$p_D(\gamma_b) = \frac{L}{\bar{\gamma}_c} \exp(-\gamma_b/\bar{\gamma}_c) [1 - \exp(-\gamma_b/\bar{\gamma}_c)]^{L-1} \quad (5.20)$$

Now the probability of bit error can be calculated for the selection diversity combining technique using DQPSK and 8-ary PSK.

For selection diversity using DQPSK,

$$P_B(\text{DQPSK, selection diversity}) = \int_0^{\infty} \frac{L}{\bar{\gamma}_c} \exp(-\gamma_b/\bar{\gamma}_c) \cdot [1 - \exp(-\gamma_b/\bar{\gamma}_c)]^{L-1} \cdot P_{B,\text{DQPSK}}(\gamma_b) d\gamma_b \quad (5.21)$$

where

$$P_{B,\text{DQPSK}}(\gamma_b) = 2Q[(4\gamma_b \sin^2(\pi/8))^{0.5}]$$

For selection diversity using 8-ary PSK,

$$P_B(\text{8PSK, selection diversity}) = \int_0^{\infty} \frac{L}{\bar{\gamma}_c} \exp(-\gamma_b/\bar{\gamma}_c) \cdot [1 - \exp(-\gamma_b/\bar{\gamma}_c)]^{L-1} \cdot P_{B,\text{8PSK}}(\gamma_b) d\gamma_b \quad (5.22)$$

where

$$P_{B,\text{8PSK}}(\gamma_b) = \frac{2}{3} Q[(6\gamma_b)^{0.5} \sin(\pi/8)]$$

Equal Gain Diversity

This diversity technique is characterized by the property that all channels have exactly the same gain (3:1081).

In terms of Eq (5.8)

$$a_j = 1, j = 1, 2, \dots, L \quad (5.23)$$

The principle of this method is that all the received channel signals, $f_j(t)$, are added together and the resulting $f(t)$ is formed (See Figure 5.3). The parameter for choosing the optimum signal is a summation of the signals (i.e., signal strengths) to determine which symbol signal was transmitted.

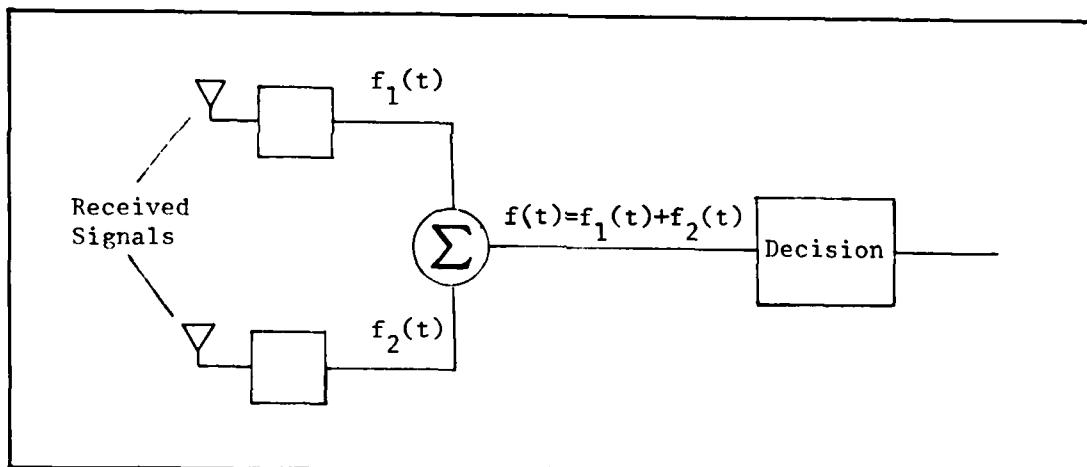


Figure 5.3 Equal Gain Diversity

Analysis of Equal Gain Diversity

The combiner output SNR with ideal equal-gain combining is

$$\gamma_b = \sum_{K=1}^L \alpha_K^2 \cdot \frac{\epsilon_b}{N_K} \quad (5.24)$$

where

α_K = attenuation factor in Kth channel

ϵ_b = energy per bit in the transmitted signal

N_K = noise spectral power density in Kth channel

L = number of diversity channels

By assuming Rayleigh fading and equal noise in all channels, the p.d.f. of γ_b for equal-gain diversity combining is developed by Schwartz et al., (20:456-7) as

$$p_D(\gamma_b) = \frac{2^{L-1} L^L (\gamma_b)^{L-1}}{(2L-1)! \prod_{K=1}^L \bar{\gamma}_{CK}} \quad (5.25)$$

where

$$\bar{\gamma}_{CK} = E\{\bar{\gamma}_{CK}\}$$

If we assume all diversity channels have equal mean SNR over the short-term fading, $\bar{\gamma}_{CK} = \bar{\gamma}_c$ then

$$p_D(\gamma_b) = \frac{2^{L-1} L^L (\gamma_b)^{L-1}}{(2L-1)! (\bar{\gamma}_c)^L} \quad (5.26)$$

Now the probability of bit error can be calculated for the equal-gain diversity combining technique using DQPSK and 8-ary PSK.

For equal-gain diversity using DQPSK,

$$P_B(\text{DQPSK, equal-gain diversity}) = \int_0^\infty \frac{2^{L-1} L^L (\gamma_b)^{L-1}}{(2L-1)! (\bar{\gamma}_c)^L} \cdot P_{B,\text{DQPSK}}(\gamma_b) d\gamma_b \quad (5.27)$$

where

$$P_{B,DQPSK}(\gamma_b) = 2Q[(4\gamma_b \sin^2(\pi/8))^{0.5}]$$

For equal-gain diversity using 8-ary PSK,

$$P_B(8PSK, \text{equal-gain diversity}) = \int_0^{\infty} \frac{2^{L-1} \gamma_b^L (\gamma_b)^{L-1}}{(2L-1)! (\bar{\gamma}_c)^L} \cdot P_{B,8PSK}(\gamma_b) d\gamma_b \quad (5.28)$$

where

$$P_{B,8PSK}(\gamma_b) = \frac{2}{3} Q[(6\gamma_b)^{0.5} \sin(\pi/8)]$$

Maximal Ratio

This diversity technique is similar to the equal gain method as the received channel signals, $f_j(t)$, are summed together to form the system output signal, $f(t)$; however, unlike the equal gain technique, maximal ratio requires that the gain of each channel is weighted by a factor proportional to its received signal strength (See Figure 5.4). Therefore, a strong received signal carries a larger weight and contributes more to the system output, $f(t)$, than a weak one. Each received channel signal is multiplied by the corresponding complex-valued (conjugate) channel gain $a_k \exp(j\phi_k)$ thus this type of combiner assumes that the channel attenuations and phase shifts are perfectly known (19:472).

Maximal ratio diversity is one of the most commonly used linear diversity combining techniques since it has been shown that it is the optimum combining method with respect to probability of error (3:1081, 9:2-8). However, to obtain the proper weighting factors for each channel requires complex instrumentation. In a satellite communications down-link, a satellite beacon could provide the information needed

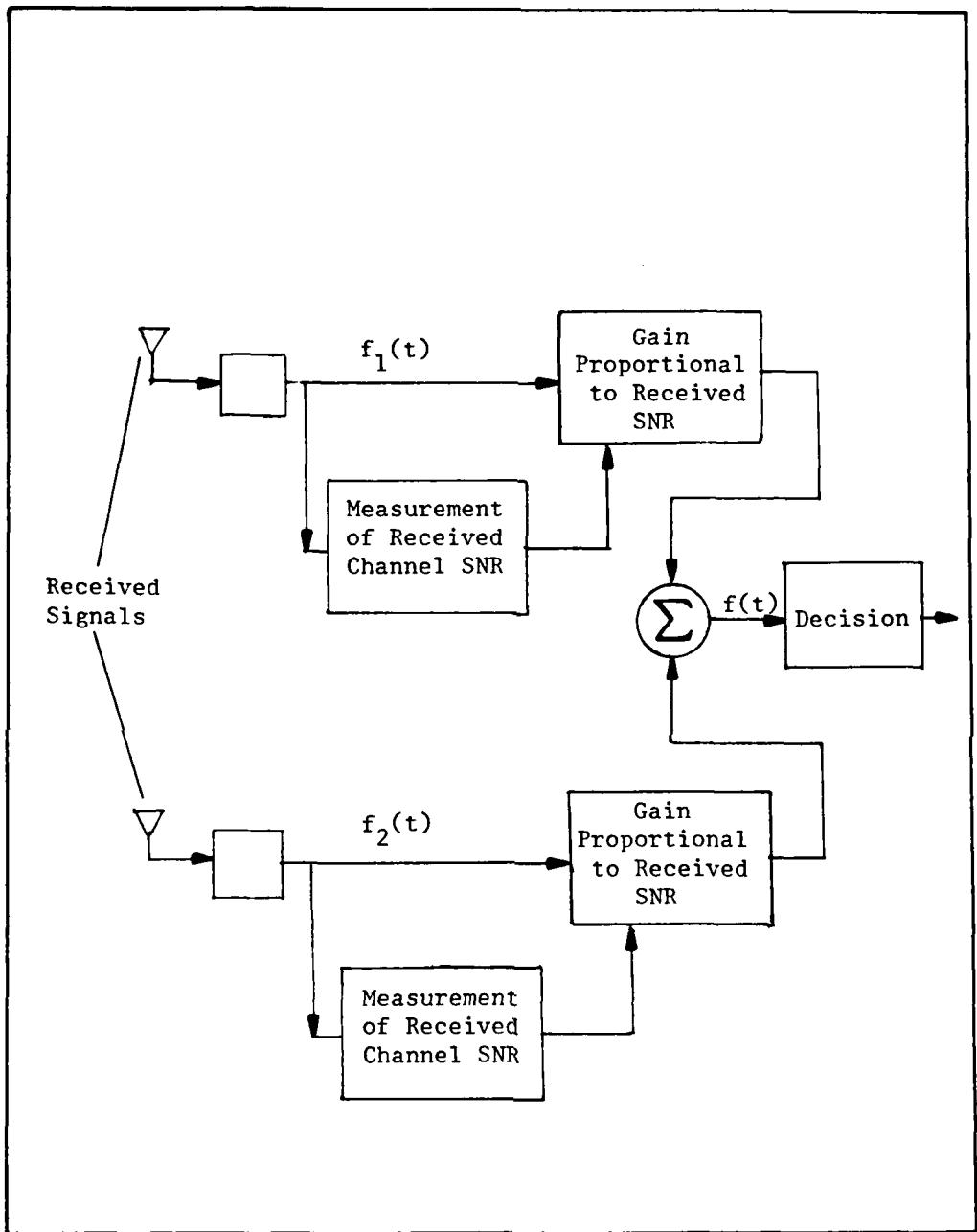


Figure 5.4 Maximal Ratio Diversity

to form the proper weighting factors. For this reason, sometimes equal gain or selection diversity is chosen since the additional advantages of maximal ratio may not be large enough to justify the additional cost of the equipment needed to achieve the necessary maximal ratio combining.

Analysis of Maximal Diversity

The p.d.f. of the output SNR, γ_b , for a maximal ratio combiner over short-term fading is developed by Schwartz et al., (20:442-4). By taking the LaPlace transform of the characteristic function of γ_b and obtaining the inversion of the transform, a complicated expression for $p_D(\gamma_b)$ is obtained via contour integration. However, for the special case when all average channel SNRs are equal during the short term fading, this expression reduces to

$$p_D(\gamma_b) = \frac{1}{(L-1)!} \frac{(\gamma_b)^{L-1}}{(\bar{\gamma}_c)^L} \exp(-\gamma_b/\bar{\gamma}_c) \quad (5.29)$$

Now the probability of bit error can be calculated for the maximal-ratio diversity combining technique using DQPSK and 8-ary PSK.

For maximal ratio diversity using DQPSK,

$$P_B(\text{DQPSK, maximal ratio diversity}) = \int_0^\infty \frac{1}{(L-1)!} \frac{(\gamma_b)^{L-1}}{(\bar{\gamma}_c)^L} \exp(-\gamma_b/\bar{\gamma}_c) \cdot P_{B,\text{DQPSK}}(\gamma_b) d\gamma_b \quad (5.30)$$

where

$$P_{B,\text{DQPSK}}(\gamma_b) = 2Q[(4\gamma_b \sin^2(\pi/8))^{0.5}]$$

For maximal ratio diversity using 8-ary PSK,

$$P_B(8\text{PSK, maximal ratio diversity}) = \int_0^\infty \frac{1}{(L-1)!} \frac{(\gamma_b)^{L-1}}{(\bar{\gamma}_c)^L} \cdot \exp(-\gamma_b/\bar{\gamma}_c) \cdot P_B, 8\text{PSK}(\gamma_b) d\gamma_b \quad (5.31)$$

where

$$P_B, 8\text{PSK}(\gamma_b) = \frac{2}{3} \Omega [(6\gamma_b)^{0.5} \sin(\pi/8)]$$

An alternative method to calculate the probability of bit error for maximal ratio diversity systems is developed by Proakis in Ref 19. Proakis (19:490) develops a general result for the probability of a symbol error in M-ary PSK systems using maximal ratio diversity

$$P_M = \frac{(-1)^{L-1} (1-\mu^2)^L}{\pi (L-1)!} \left\{ \frac{1}{b-u^2} \left[\frac{\pi}{M} (M-1) - \frac{u \sin(\pi/M)}{[b-u^2 \cos^2(\pi/M)]^{0.5}} \cot^{-1} \left(\frac{-\mu \cos \cos(\pi/M)}{[b-u^2 \cos^2(\pi/M)]^{0.5}} \right) \right] \right\} \quad (5.32)$$

where

$$\mu = [\bar{\gamma}_c / (1 + \bar{\gamma}_c)]^{0.5} \text{ for coherent PSK}$$

$$\mu = \bar{\gamma}_c / (1 + \bar{\gamma}_c) \text{ for DPSK}$$

$$\bar{\gamma}_c = \text{average SNR per channel} = \frac{E \{ \alpha_K^2 \} \epsilon}{N_0}$$

ϵ = energy in transmitted signal

$$\gamma_b = \text{average bit SNR} = \frac{L \bar{\gamma}_c}{K}$$

$$K = \log_2 M$$

The bit error rate for DQPSK with maximal ratio diversity is derived by Proakis assuming a Gray code (See Figure 5.5). The probability of bit error is calculated by

$$P_B(\text{DQPSK, maximal ratio diversity}) = \sum_{K=1}^2 (K \text{ errors}) \cdot (P_{eK}) \quad (5.33)$$

where

P_{eK} = probability of error for K bit errors

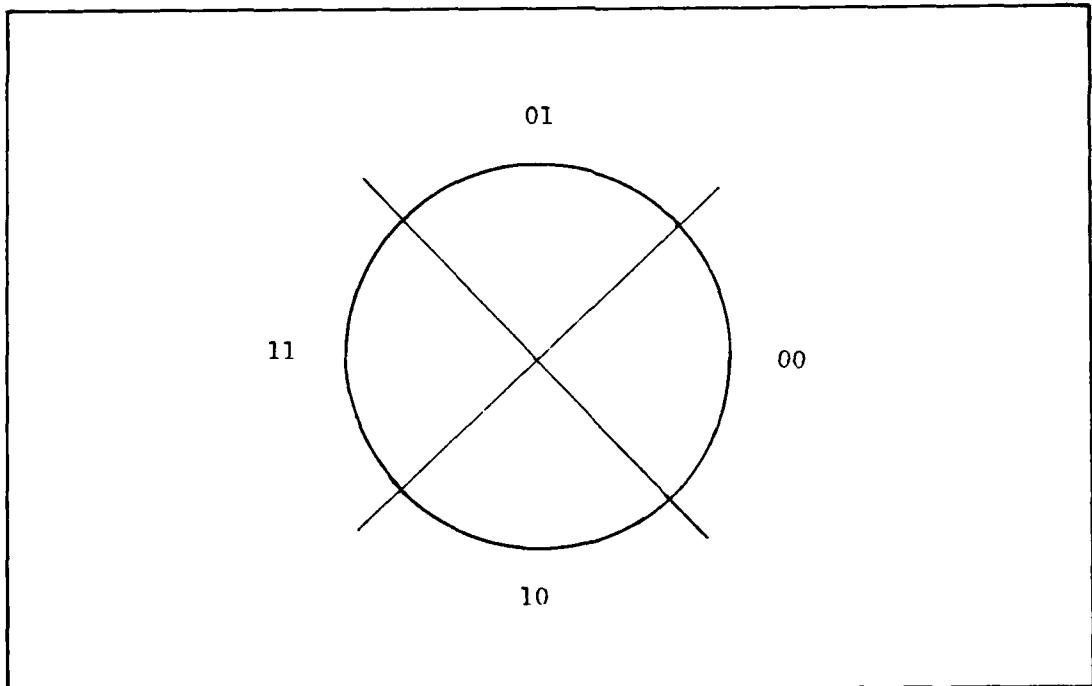


Figure 5.5 4-ary Gray Code

The resulting expression for probability of bit error for DQPSK with maximal ratio diversity is

$$P_B(\text{DQPSK, maximal ratio diversity}) = 0.5 \left[1 - \frac{\mu}{(2-\mu^2)^{0.5}} \sum_{K=0}^{L-1} \binom{2K}{K} \frac{(1-\mu^2)^K}{4-2\mu} \right] \quad (5.34)$$

where

$$\mu = [\bar{\gamma}_c / (1 + \bar{\gamma}_c)]^{0.5}$$

Using the same method used by Proakis for obtaining Eq (5.34), the probability of bit error for an 8-ary PSK signal with maximal ratio diversity can be generated by evaluating Eq (5.5) where

$\int_{\theta_1}^{\theta_2} 2 P(\theta) d\theta$ is defined by Proakis [Eq (7A.14), Ref 19:532] as

$$\int_{\theta_1}^{\theta_2} 2 p(\theta) d\theta = \frac{(-1)^{L-1} (1-\mu^2)^L}{2\pi(L-1)!} \frac{\partial^{L-1}}{\partial b^{L-1}} \left(\frac{1}{b-\mu} \right) \left\{ \frac{\mu(1-[b/\mu^2]-1)x^2}{b^{0.5}} \right. \\ \left. \cdot \cot^{-1}x - \cot^{-1}\left(\frac{(xb^{0.5}/\mu)}{1-[b(\mu^2)-1]x^2} \right)^{0.5} \right\} \Big|_{x_1}^{x_2} \Big|_{b=1} \quad (5.35)$$

where

$$x_i = \frac{-\mu \cos \theta_i}{(b-\mu^2 \cos \theta_i)^{0.5}}, \quad i = 1, 2$$

$$\mu = [\bar{\gamma}_c / (1 + \bar{\gamma}_c)]^{0.5}$$

VI. Computer Program Development

Having developed the equations needed to calculate the probability of bit error for the different combinations of diversity techniques and digital signaling schemes, it was necessary to develop a computer program to obtain the desired calculations. In order to reduce run time, I wrote a separate program in Fortran 77 for each diversity technique/digital signaling scheme combination. Including the case of no diversity (i.e., the probability of bit error for DQPSK and 8-ary PSK with no diversity), there are seven programs used to calculate the probability of bit error calculations.

Choice of Range of Variables

The computer results were to be plotted as the probability of bit error versus the signal-to-noise ratio (SNR) per bit. Therefore, a range for the SNR per bit needed to be chosen. Considering the range (5-40 dB) chosen in similar graphs presented in Ref 19, the range for bit SNR was chosen as 10-40 in decibels. A determination was also made on the maximum number of diversity channels for probability of error calculations. Since the use of more than two diversity channels in a satellite communications diversity system is rare, I limited the probability of bit error calculations for the six different diversity/signaling scheme combinations to 2, 3, and 4 diversity channels. Therefore, the final results for the six combinations can be compared over the bit SNR

range of 10-40 decibels for 2, 3, and 4 diversity terminals. Likewise, these results can be compared to the case of no diversity to determine the benefits of the diversity system.

Equations Used to Calculate Probability of Bit Error

The equations needed to calculate the probability of bit error for all of the diversity/signaling scheme combinations were developed in Section V. The equations from Section V used in the computer programs are listed below:

DQPSK w/no diversity Eq (5.10)

8-ary PSK w/no diversity Eq (5.11)

Selection diversity w/DQPSK Eq (5.21)

Selection diversity w/8-ary PSK Eq (5.22)

Equal Gain diversity w/DQPSK Eq (5.27)

Equal Gain diversity w/8-ary PSK Eq (5.28)

Maximal Ratio diversity w/DQPSK Eq (5.30)

Maximal Ratio diversity w/8-ary PSK Eq (5.31)

All of the equations listed above require the solution to an indefinite integral. For the maximal ratio case, an alternative method for obtaining the probability of bit error for DQPSK and 8-ary PSK is stated in Eqs (5.34) and (5.35), respectively. The difficulties in getting the required partial derivatives for this method resulted in the deletion of this method.

Solving the Indefinite Integral

The choice of Fortran 77 as the programming language for the programs for calculating the probability of bit error was primarily due to the mathematical and statistical library available in Fortran. In order to solve the indefinite integrals needed to find the probabilities of bit error, I used the DCADRE subroutine from the IMSL software library. The DCADRE subroutine performs a numerical integration of a function using cautious adaptive Romberg extrapolation.

The indefinite integrals in the equations for evaluating the probability of error were approximated by using a piecewise summation of the integration. The integral from zero to infinity is approximated by the piecewise integral from 1×10^{-15} to the point where the area of this last subinterval is less than 0.000001 of the summation of its area plus all previously calculated subinterval areas. This approximation works satisfactorily since the product of the p.d.f. of the diversity technique and the conditional probability of bit error given the bit SNR is always positive and the limit of this product approaches zero as bit SNR approaches infinity.

The DCADRE subroutine requires that the integrand of the integral be supplied by the user in the form of a function. For each diversity/signaling scheme combination, the product of the p.d.f. and conditional probability was expressed as a Fortran function so the DCADRE function could calculate the subinterval area. In order to calculate the conditional

probability of a bit error for the digital signaling scheme within this function, another subroutine from the IMSL software library was needed.

The IMSL subroutine MERFD=DERF was used to evaluate the mathematical error function of a double precision argument. This subroutine computes the value of the integral

$$\text{derf}(Y) = (2/\pi) \int_0^Y \exp(-t^2) dt \quad (6.1)$$

where

Y = argument of the mathematical error function

By performing the following conversion, the Q function defined by Eq (2.25.a) can be expressed as a function of the IMSL subroutine MERFD=DERF.

$$Q(x) = 1 - [(\text{derf}(x/2^{0.5}) + 1)/2] \quad (6.2)$$

Therefore, the conditional probabilities in the integrand of the indefinite integral can be expressed in the Q function form within the Fortran function needed by the DCADRE subroutine.

Validation of Computer Results

The computer results for the DQPSK with no diversity and DQPSK with maximal ratio diversity cases were compared to the results presented by Proakis in Ref G, Chapter 7. For each case, the results were similar, although my probability of bit error curves are slightly shifted to the right of Proakis' curves (i.e., for both cases my results show

slightly higher probability of bit error rates than Proakis). The most likely cause of this difference is the approximation used for DQPSK [Eq (5.2)]. However, the accuracy of the computer results is well within the range to validate the approach used to compute the probability of bit error. Since all seven programs were written using the same approach, it is assumed that all the computer results are reasonably accurate and in particular, the results are accurate for assessing the relative performance of the diversity schemes.

Computer Program for Calculation of Rain Attenuation

In addition to the programs for calculating the probability of bit error, a program was developed to calculate the attenuation per unit distance, A, based on the approximate relation between A and the rain rate R, where $A = aR^b$, described in Eq (3.2). The values for the coefficients a and b were obtained for three different rain temperatures, -10°C , 0°C , and 20°C . These values were obtained from Tables 3.2, 3.3, and 3.4 using a downlink frequency of 20 GHz and a Marshall-Palmer (MP) raindrop size distribution. The rain attenuation per unit distance will be calculated as decibels/kilometers and the rain rate will vary from 5 mm/hr to 100 mm/hr.

VII. Results

The data obtained from the computer programs described in Section VI are discussed in the following pages. By examining the data, an evaluation of the different diversity/signaling scheme combinations can be obtained to determine the benefits of using a diversity network. Comparisons between the different diversity techniques will illustrate which technique yields the maximum benefits.

Analysis of Diversity Benefits

By using the HP-7229 plotter, the results of the computer programs were plotted to obtain the graphs of the probability of bit error versus the SNR per bit for each diversity/signaling scheme combination. These graphs are depicted in the following figures:

DQPSK and 8-ary PSK
w/No Diversity

Figure 7.1

Selection Diversity
w/DQPSK

Figure 7.2

Selection Diversity
w/8-ary PSK

Figure 7.3

Equal Gain Diversity
w/DQPSK

Figure 7.4

Equal Gain Diversity
w/8-ary PSK

Figure 7.5

Maximum Ratio Diversity
w/DQPSK

Figure 7.6

Maximum Ratio Diversity
w/8-ary PSK

Figure 7.7

By looking at Figures 7.1 - 7.7, it is obvious that the use of a diversity technique greatly reduces the probability of bit error in a Rayleigh fading channel. It is also apparent that regardless of which diversity/signaling scheme is used, the probability of bit error reduces as the order of diversity of channels increases. A more indepth look at the diversity benefits are depicted in Tables 7.1 - 7.4.

As displayed in Tables 7.1 and 7.2, the benefits of diversity techniques are significant. Table 7.1 shows the benefits of the selected diversity techniques with DQPSK compared to DQPSK without diversity and Table 7.2 shows the benefits of the selected diversity techniques with 8-ary PSK compared to 8-ary PSK without diversity. For each case, as the average SNR per bit increases, the benefits of the diversity network increases. For example, given a received average bit SNR of 40 dB for a DQPSK (8-ary PSK) w/no diversity system, the minimum diversity gain is 18.25 dB (20.0 dB) when using selection diversity with two channels and the maximum diversity gain is 26 dB (27.25 dB) when using maximal ratio diversity with four channels. Likewise, for a received average bit SNR of 60 dB, the diversity gain for selection diversity with two channels is 28.25 dB (30.0 dB) and the diversity gain for maximal ratio diversity with four channels is 40.5 dB (41.75 dB).

The data displayed in Tables 7.3 and 7.4 allows for a comparison of all six diversity/signaling scheme combinations.

Two significant conclusions can be made from this data:

1. The maximal ratio diversity technique provides the most diversity gain, followed by equal gain diversity and lastly selection diversity.

2. The diversity/signaling scheme combinations with 8-ary PSK outperform the same combinations with DQPSK.

(The latter conclusion may partially result from the approximation used for DQPSK). Based on these results, the optimum diversity/signaling scheme combination of the six is the maximal ratio diversity technique with 8-ary PSK.

Other important considerations regarding the selection of a diversity technique for a satellite communications system is the cost of implementing the diversity technique. As denoted in Section V, maximal ratio diversity requires the use of a satellite beacon to properly weigh the received channel signals. Although maximal ratio diversity provides the best diversity gain, it is also the most costly to implement due to the additional equipment needed to obtain the satellite beacon information and translate it into correct weighing factors. Thus, there is a direct trade-off between cost and performance in the selection of the diversity technique and the number of earth stations used in the satellite communications diversity system.

Analysis of Rain Attenuation for Downlink

The rain attenuation for a satellite communications downlink can be estimated from the data presented in Figures 7.8

and 7.9. In Figure 7.8, the rain attenuation per unit distance (dB/km) can be approximated by knowing the rain rate for rain temperatures of 20°C, 0°C, and -10°C. Given the rain rate and the angle of elevation of the receiving satellite terminal, the effective path length (in km) can be estimated using Figure 7.9.

Therefore, the approximate rain attenuation (in dB) can be obtained by multiplying the effective path length determined from Figure 7.9 and the rain attenuation per unit distance indicated from Figure 7.8. By knowing the approximate rain attenuation, its effect on the probability of a bit error can be determined from Figures 7.1 - 7.7. By subtracting the rain attenuation from a given received bit SNR for a diversity/signaling scheme for a satellite communications downlink without rainfall effects, the corresponding probability of bit error can be obtained. The increase in the probability of bit error is the result of the rain attenuation. Therefore, the effects of rain attenuation for different rain rates and different elevation angles on the six different diversity/signaling scheme combinations can be estimated using Figures 7.1 - 7.9.

For example, assume a maximal ratio diversity system with two channels using 8-ary PSK for a downlink earth station with an angle of elevation of 40° operating during clear weather conditions. For an average received SNR per bit of 20 dB, the probability of bit error obtained from Figure 7.7 is 2.807×10^{-5} . Now assume a rain rate of 25 mm/hr and a

rain temperature of 20°C. From Figure 7.8, the rain attenuation is ~ 2.6 dB/km and from the effective path length of ~ 4.4 km is obtained from Figure 7.9. Thus, the rain attenuation is ~ 11.44 dB and the effective average received SNR per bit for the diversity system is now ~ 9.5 dB with a probability of bit error of 2.786×10^{-3} . Obviously, the detrimental effect of rain attenuation on the performance of satellite communications systems is very significant.

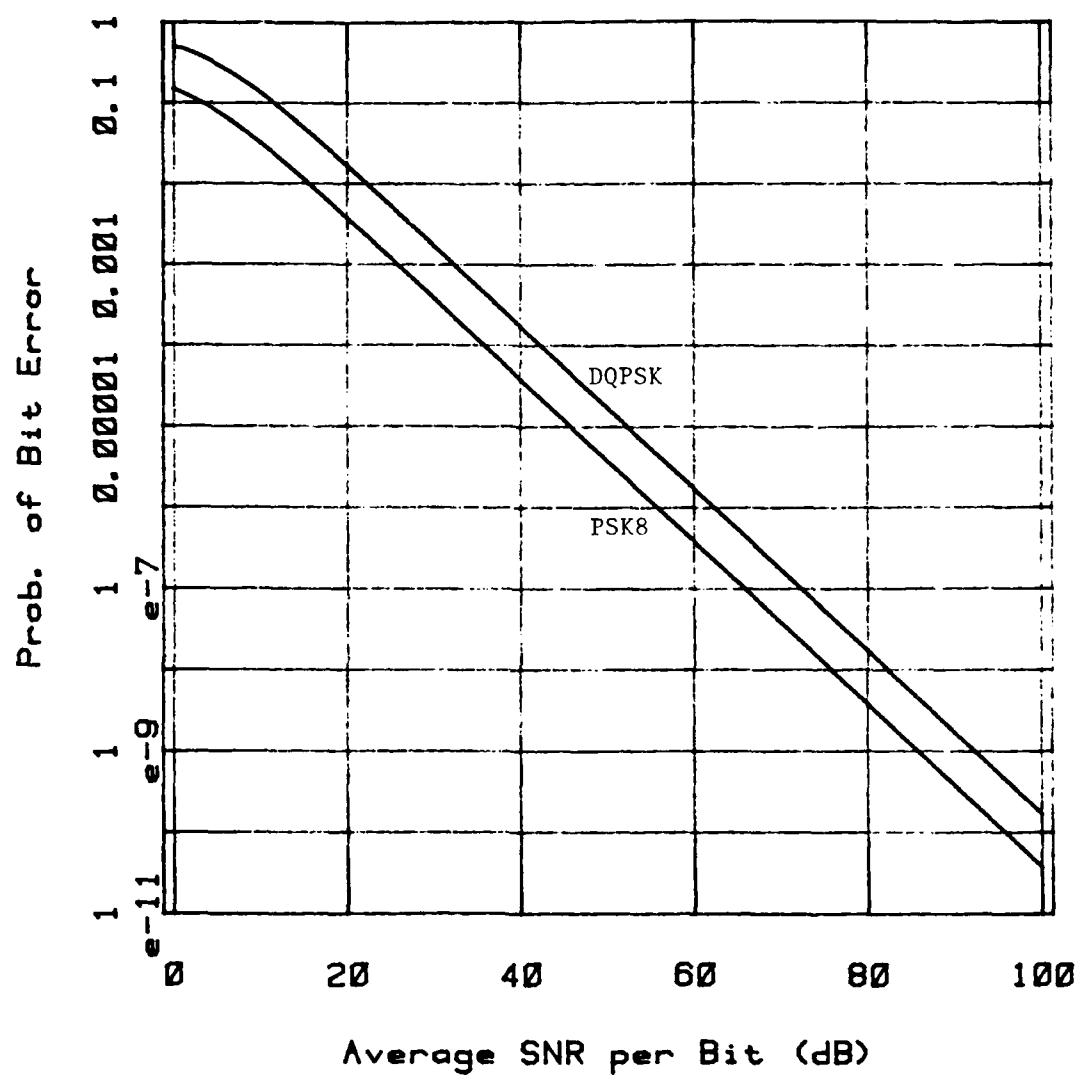


Figure 7.1 DQPSK and 8-ary PSK w/No Diversity

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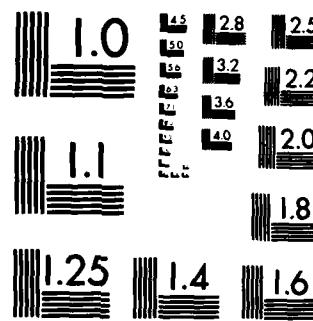
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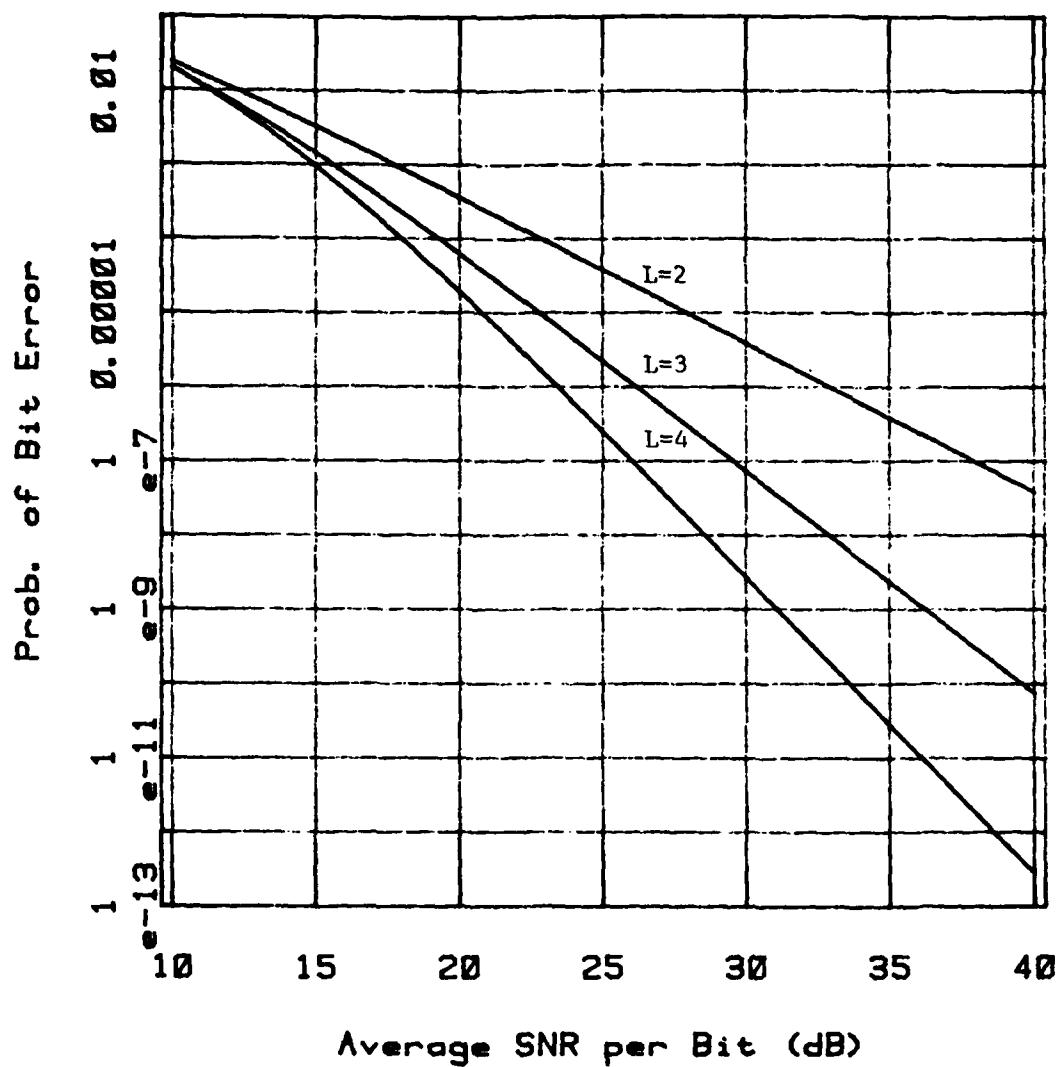


Figure 7.2 Selection Diversity w/DQPSK

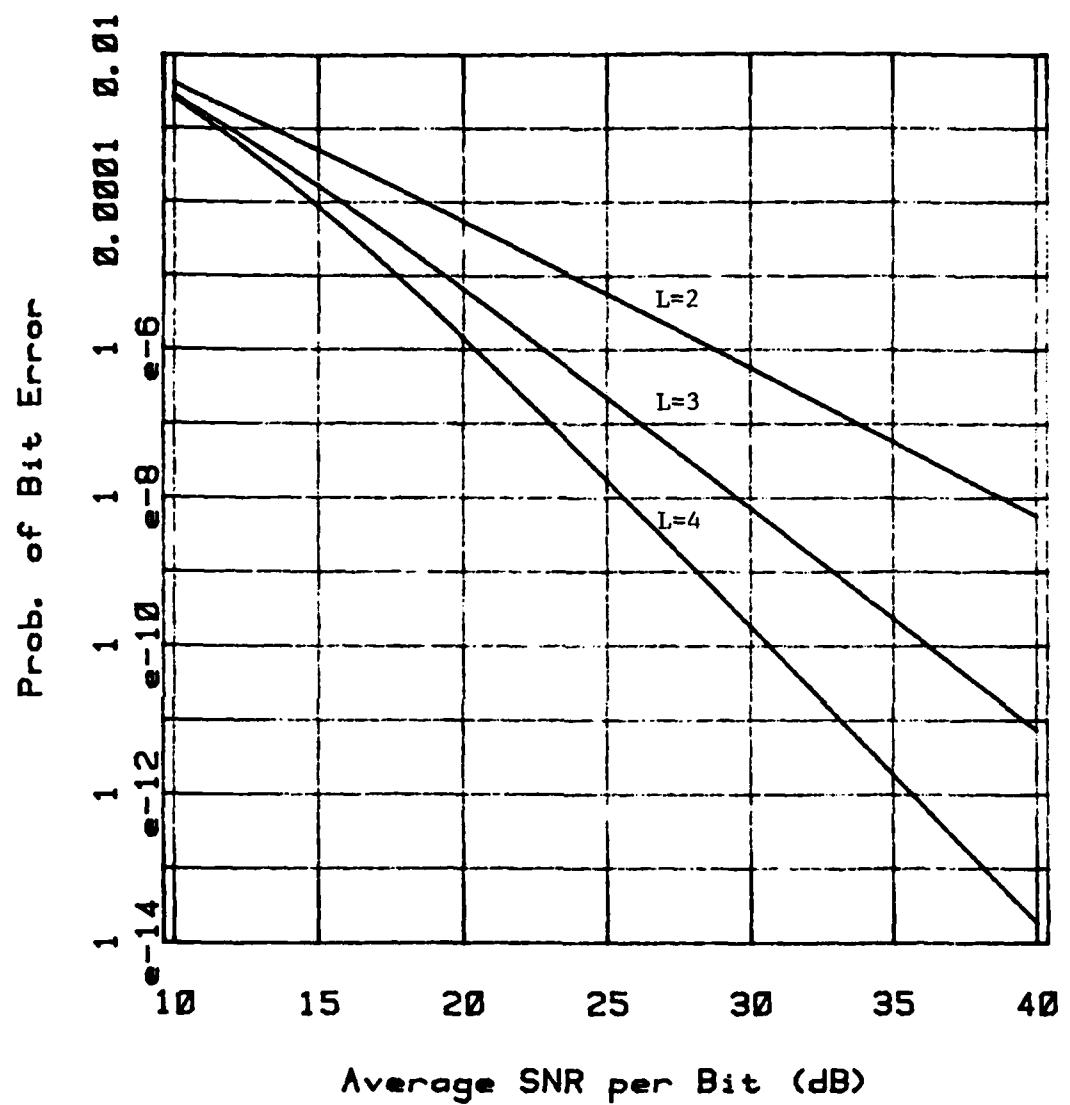


Figure 7.3 Selection Diversity w/8-ary PSK

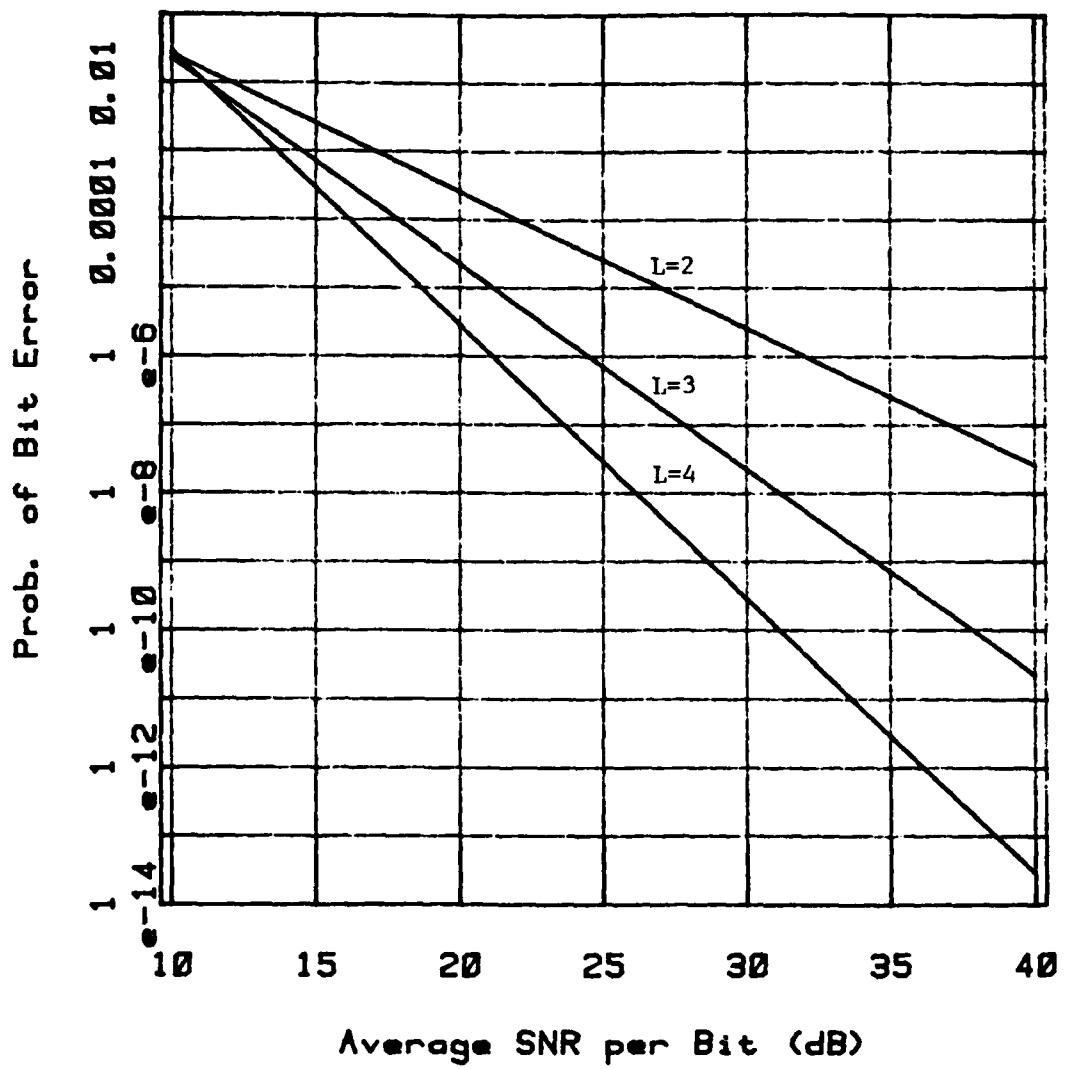


Figure 7.4 Equal Gain Diversity w/DQPSK

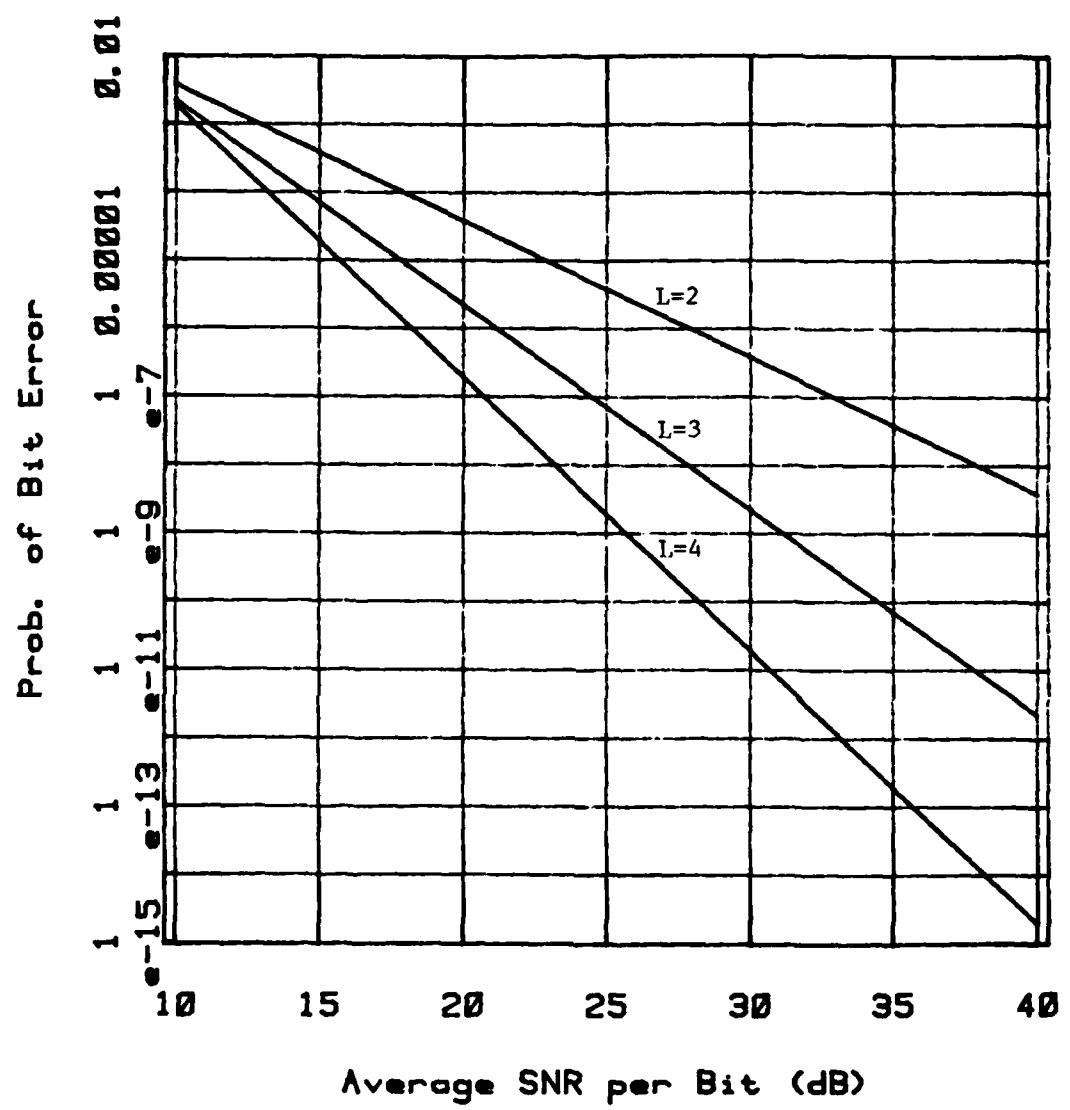


Figure 7.5 Equal Gain Diversity w/8-ary PSK

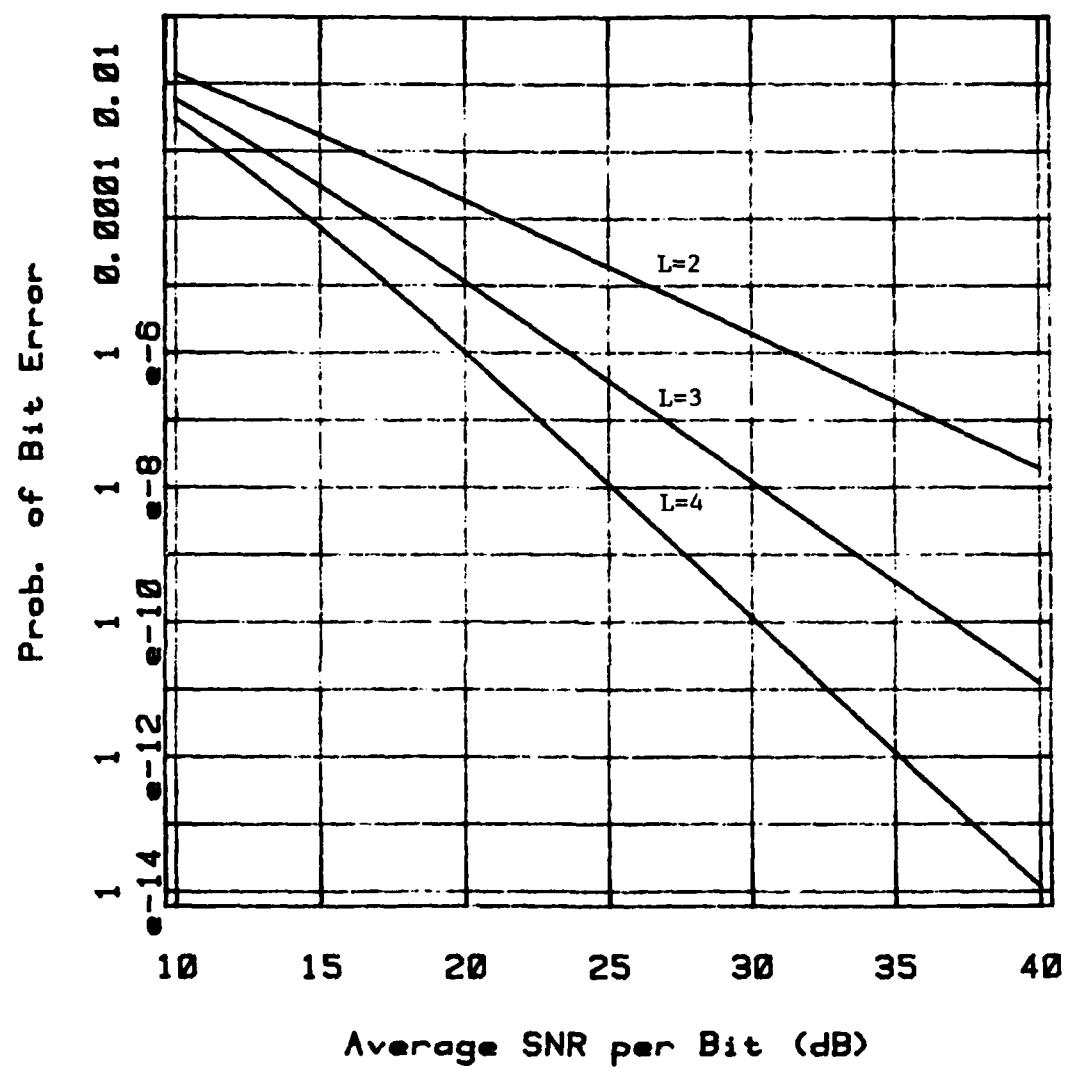


Figure 7.6 Maximal Ratio Diversity w/DQPSK

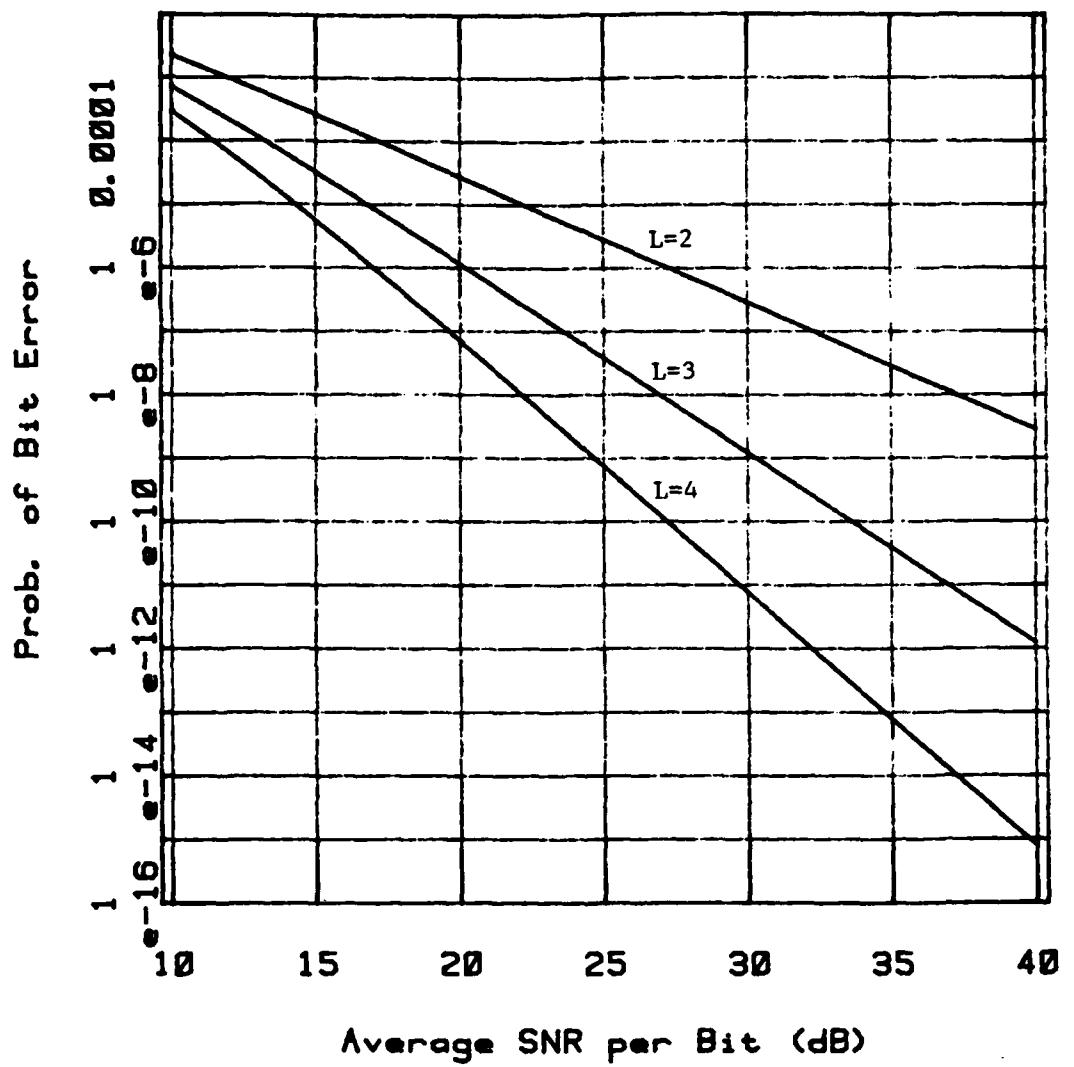


Figure 7.7 Maximal Ratio Diversity w/8-ary PSK

TABLE 7.1
Comparison of Selected Diversity Techniques w/DQPSK to DQPSK w/No Diversity

		Probability of Bit Error			
		1.660 x 10 ⁻²	1.702 x 10 ⁻⁴	1.703 x 10 ⁻⁶	1.703 x 10 ⁻⁸
DQPSK w/no Diversity		20.0dB	40.0dB	60.0dB	80.0dB
2 channels	11.0	21.75	31.75	41.75	51.75
3 channels	10.5	18.5	25.25	32.0	39.5
4 channels	10.5	17.25	22.75	28.0	33.25
2 channels	11.5	20.75	31.0	41.0	51.0
3 channels	10.75	17.0	23.75	30.25	37.75
4 channels	10.75	15.5	20.5	25.5	30.75
2 channels	9.5	20.25	30.25	40.25	50.25
3 channels	8.0	16.0	22.75	29.5	36.5
4 channels	7.25	14.0	19.5	24.5	29.75

Average $\frac{E_b}{N_0}$ Needed to Achieve Prob. of Bit Error Performance

TABLE 7.2
Comparison of Selected Diversity Techniques w/8-ary PSK to 8-ary PSK w/No Diversity

Probability of Bit Error						
	3.720×10^{-3}	3.783×10^{-5}	3.784×10^{-7}	3.784×10^{-9}	3.784×10^{-11}	
8-ary PSK w/ no Diversity	20.0dB	40.0dB	60.0dB	80.0dB	100.0dB	
2 channels	10.25	21.0	31.0	40.75	51.25	
3 channels	9.5	17.25	24.25	31.0	37.75	
4 channels	9.25	16.0	21.5	26.75	31.75	
SELECTION DIVERSITY						
2 channels	10.0	20.0	30.0	40.0	50.0	
3 channels	9.25	16.0	22.5	29.25	36.0	
4 channels	9.25	14.25	19.25	24.25	29.25	
EQUAL GAIN DIVERSITY						
2 channels	8.75	19.25	29.5	39.75	49.25	
3 channels	7.0	14.75	21.75	28.5	35.5	
4 channels	6.0	12.75	18.25	23.25	28.5	
MAXIMAL RATIO DIVERSITY						

Average $\frac{E_b}{N_0}$ Needed to Achieve Prob. of Bit Error Performance

TABLE 7.3

Comparison of Selected Diversity Techniques w/DQPSK
with Respect to Probability of Bit Error

		Probability of Bit Error					
		10^{-3}	10^{-4}	10^{-6}	10^{-8}	10^{-10}	10^{-12}
2 channels	17.75dB	23.0dB	33.0dB	43.0dB	53.0dB	63.0dB	
3 channels	15.5	19.25	26.25	33.0	39.5	46.25	
4 channels	15.0	18.0	23.5	28.5	33.5	38.5	
2 channels	17.0	22.0	32.0	42.0	52.0	62.0	
3 channels	14.5	17.75	24.5	31.25	37.75	44.5	
4 channels	13.75	16.25	21.25	26.25	31.25	36.25	
2 channels	16.25	21.25	31.5	41.5	51.5	61.5	
3 channels	13.0	16.75	23.5	30.25	37.0	43.75	
4 channels	25.25	14.5	20.0	25.0	30.25	35.25	

Average $\frac{E_b}{N_o}$ Needed to Achieve Prob. of Bit Error Performance

TABLE 7.4

Comparison of Selected Diversity Techniques w/8-ary PSK
with Respect to Probability of Bit Error

Maximal Rate	Equal Gain	Diversity	Selection	Probability of Bit Error				
				10^{-3}	10^{-4}	10^{-6}	10^{-8}	10^{-10}
2 channels	13.5dB	18.75dB	28.75dB	38.75dB	48.75dB	58.75dB		
3 channels	12.0	15.75	22.75	29.5	36.25	43.0		
4 channels	11.5	14.75	20.5	25.5	30.75	35.75		
2 channels	13.0	18.0	28.0	37.75	48.0	58.0		
3 channels	11.25	14.5	21.25	27.75	34.5	41.25		
4 channels	10.75	13.25	18.25	23.25	28.25	33.25		
2 channels	12.0	17.0	27.25	37.25	47.25	57.25		
3 channels	9.5	13.25	20.25	27.0	33.5	40.25		
4 channels	8.25	11.5	17.0	22.5	27.25	32.50		

Average $\frac{E_b}{N_0}$ Needed to Achieve Prob. of Bit Error Performance

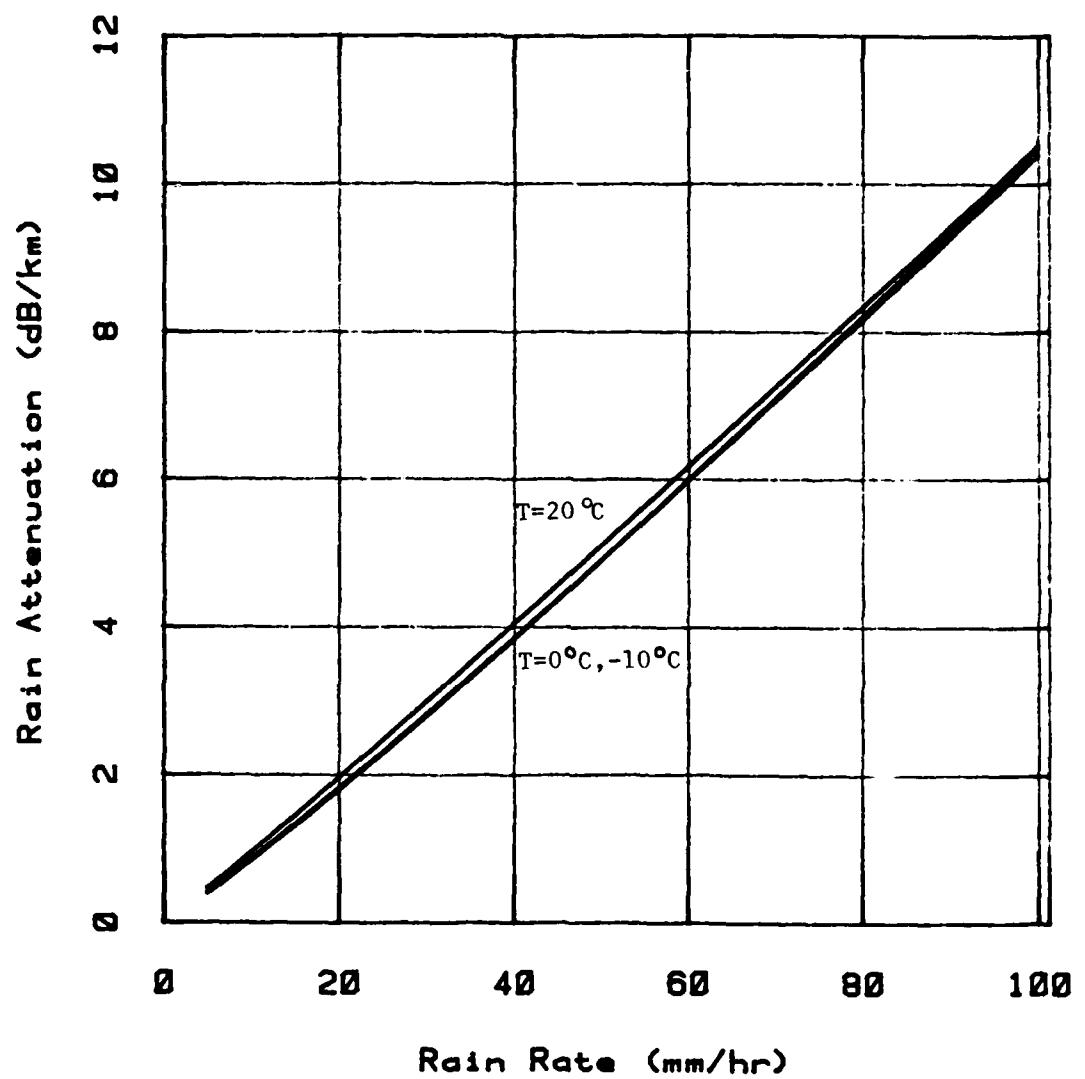


Figure 7.8 Rain Attenuation Using $A = aR^b$ Relationship

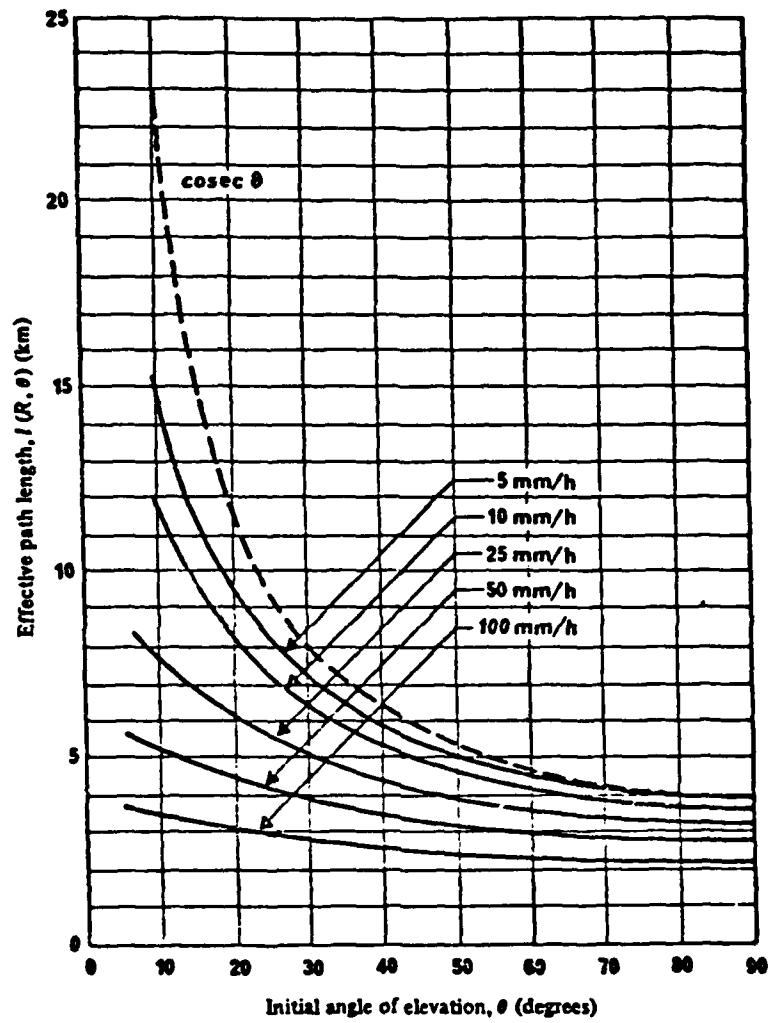


Figure 7.9 Effective Path Length for Rain Rates

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VIII. Conclusions and Recommendations

Conclusions

On the basis of the computer results of the performance of diversity techniques in the downlink reception equipment for satellite communications systems, the following conclusions are made:

1. The best link parameter to use in the process of determining the received signal in a diversity system is the received channel SNR or some variation of it such as average SNR per bit.
2. Of the three diversity techniques evaluated, maximal ratio diversity provided the optimum diversity benefits followed by equal gain diversity and lastly selection diversity. However, all three diversity methods provide significant improvement of bit error performance when compared to a similar system without diversity. These diversity combining techniques can be used to combat rain attenuation or to improve the overall reception characteristics.
3. Regardless of which diversity technique is used, as the number of channels used increases, the bit error performance improves.
4. Maximal ratio diversity requires the use of a satellite beacon while equal gain and selection diversity do not. Thus, additional equipment is needed in a maximal ratio diversity reception system thereby increasing the cost.

5. The diversity/signaling combinations using 8-ary PSK provided a slightly better bit error performance than its counterpart using DQPSK.

6. The effects of rain attenuation on a diversity downlink reception system can be estimated by applying the results of this study.

Recommendations

Based on the observations made during this investigation, the following recommendations are proposed for further study:

1. This study assumed perfect synchronization; the effects of the loss of synchronization on bit error performance should be investigated.
2. The results of this study could be applied to rainfall statistics to obtain theoretical long-range uptime and downtime statistics for downlink diversity reception systems located in various geographical locations.

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This study investigated some of the diversity combining techniques that can be used with a space diversity downlink reception configuration to overcome the attenuation effects of rainfall. The diversity combining techniques selected for development and analysis were selection, equal gain, and maximal ratio combining. Each of these techniques were considered with two different digital signaling schemes, 8-ary phase-shift keying (PSK) and differentially encoded quadrature PSK (DQPSK), to form six distinct diversity technique/signaling scheme combinations.

The analysis was accomplished by deriving the probability of bit error functions for 8-ary PSK and DQPSK and by developing the probability of density functions for each diversity technique under the assumption of a slowly fading Rayleigh channel. By taking the integral from zero to infinity of the product of the two functions for each diversity technique/signaling scheme combination, the probability of bit error was calculated for each specified combination. The number of channels in the diversity system was varied to illustrate the trade-off between the improvement of bit error performance and cost. The results show the theoretical benefits attributed to the diversity combining techniques that can be employed in satellite communications systems. Additionally, information is provided to estimate the rain attenuation given the rain rate so that its effects on bit error performance can be obtained and compared to the case of no rain attenuation.

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